

Principles of Micro- and Nanofabrication for Electronic and Photonic Devices

Doping 掺杂

Xing Sheng 盛兴

Department of Electronic Engineering
Tsinghua University

xingsheng@tsinghua.edu.cn



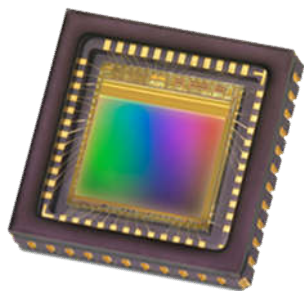
Semiconductor PN Junctions



LEDs



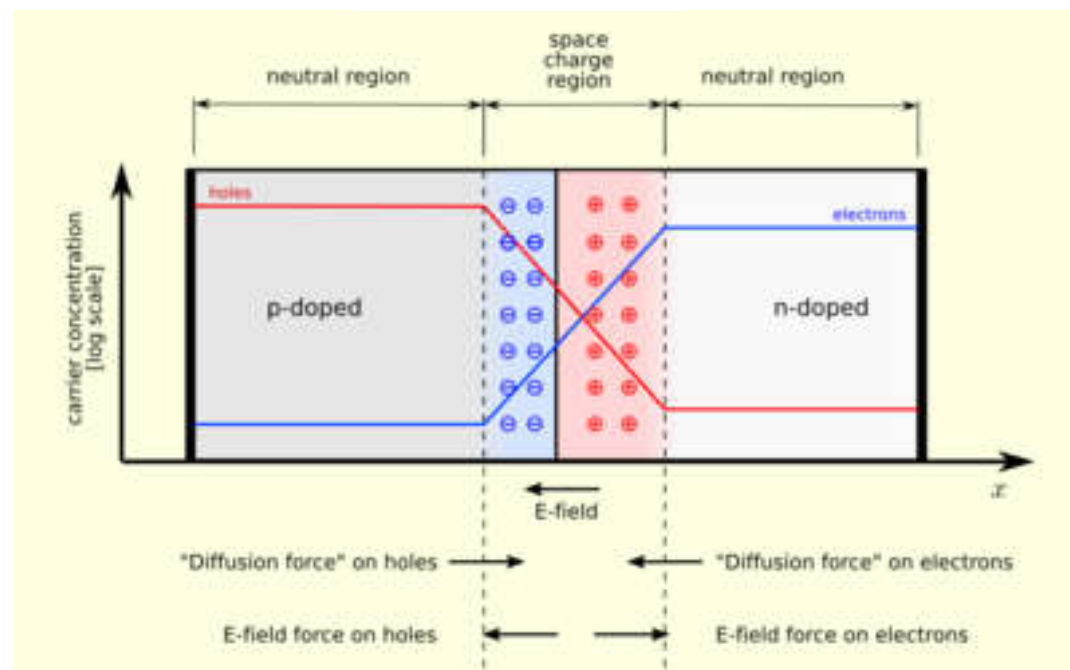
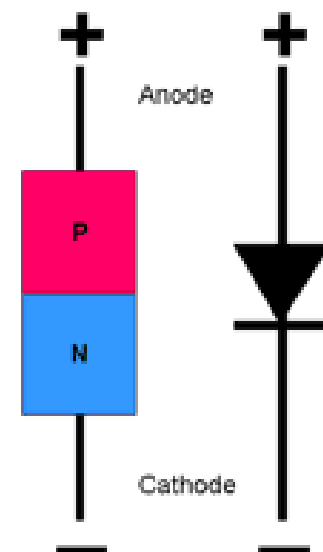
lasers



detectors

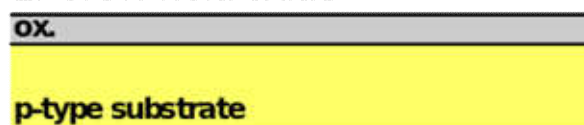


solar cells

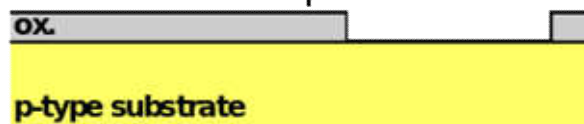


CMOS Transistors

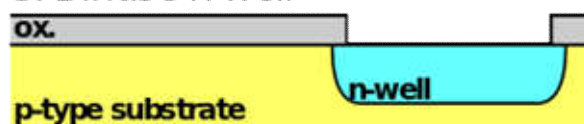
1. Grow field oxide



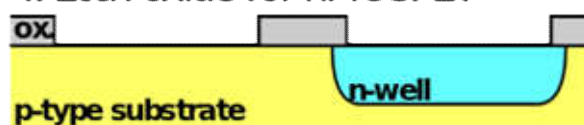
2. Etch oxide for pMOSFET



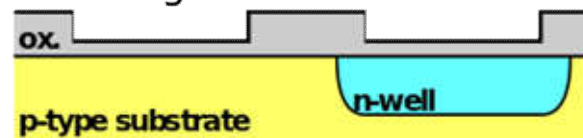
3. Diffuse n-well



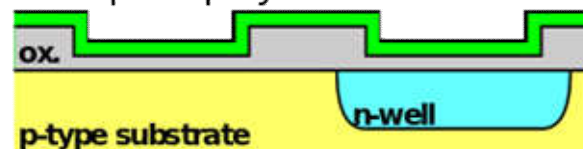
4. Etch oxide for nMOSFET



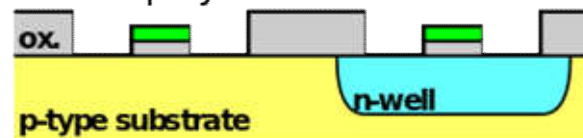
5. Grow gate oxide



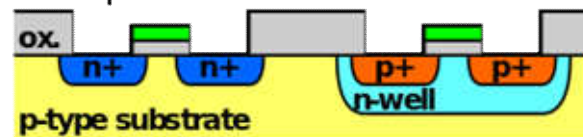
6. Deposit polysilicon



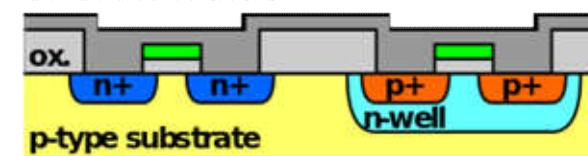
7. Etch polysilicon and oxide



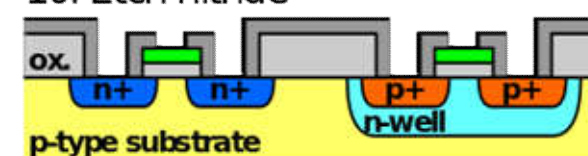
8. Implant sources and drains



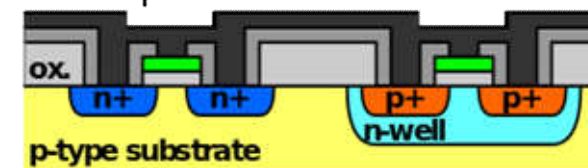
9. Grow nitride



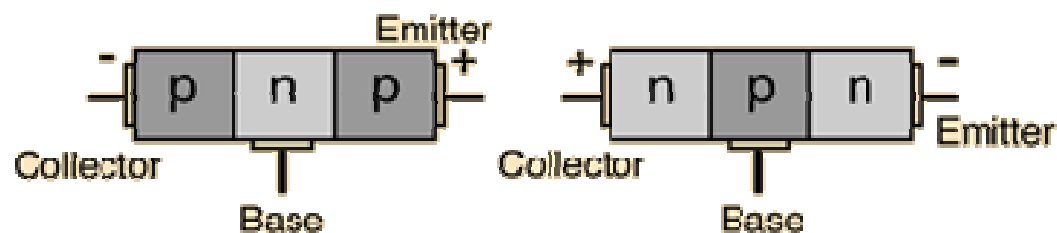
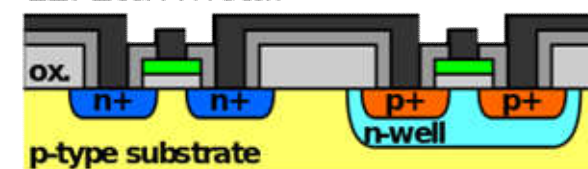
10. Etch nitride



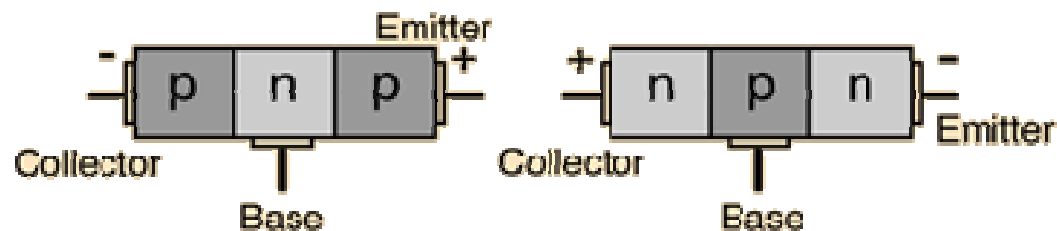
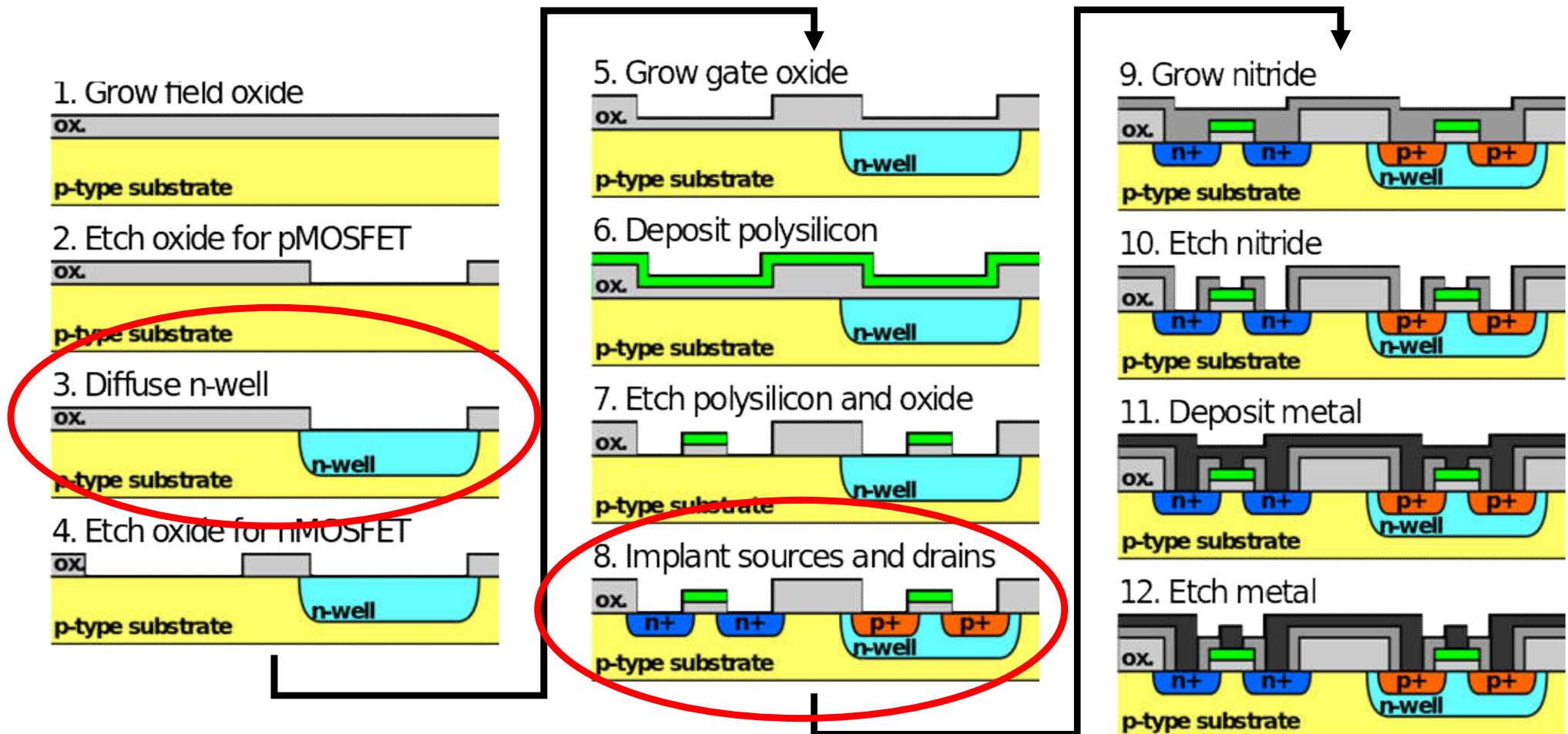
11. Deposit metal



12. Etch metal



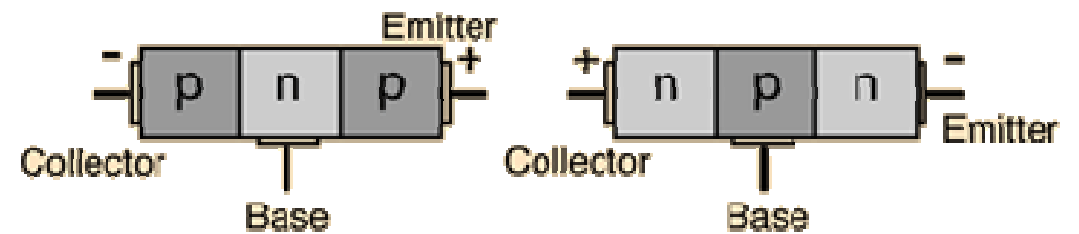
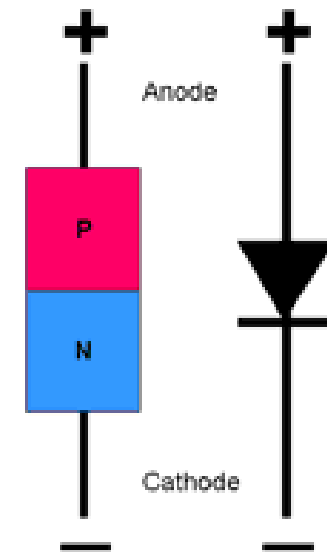
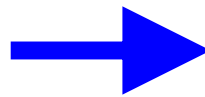
CMOS Transistors



Doping



ingots and wafers



Doping in Silicon

For silicon:

p dopant: **B, Al, Ga, ...**

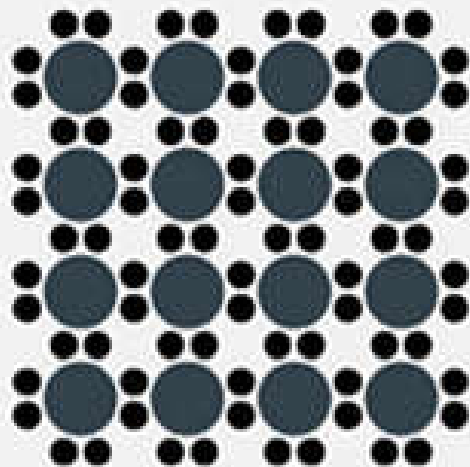
n dopant: **P, As, Sb, ...**

germanium is similar to Si.

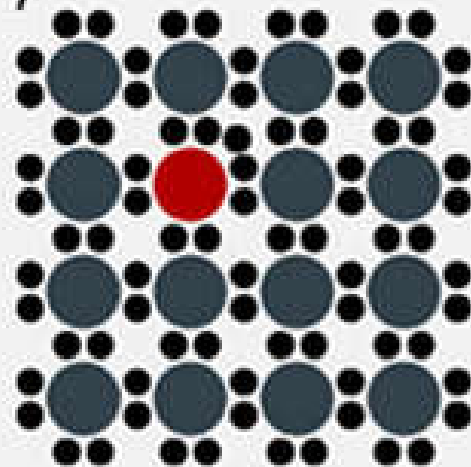
					2
B	C	N	O	F	Ne
13	14	15	16	17	18
Al	Si	P	S	Cl	Ar
31	32	33	34	35	36
Ga	Ge	As	Se	Br	Kr
49	50	51	52	53	54
In	Sn	Sb	Te	I	Xe
81	82	83	84	85	86
Tl	Pb	Bi	Po	At	Rn

Silicon
 Electron
 Phosphorus
 Boron

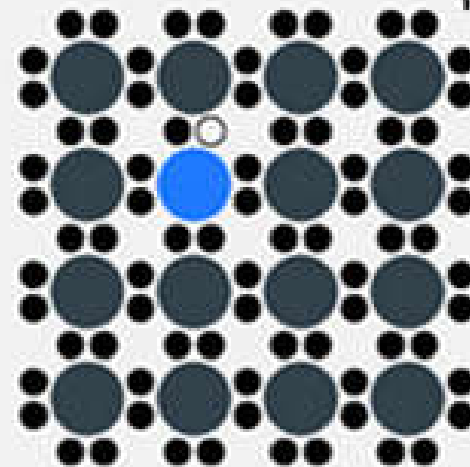
doped semiconductor



Array of Si atoms



n-type semiconductor



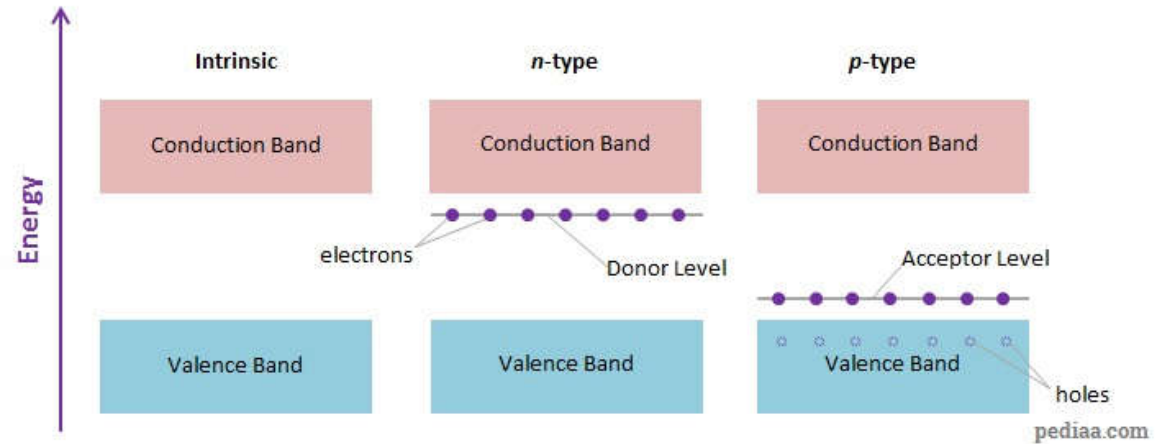
p-type semiconductor

Doping in Silicon

For silicon:

p dopant: **B, Al, Ga, ...**

n dopant: **P, As, Sb, ...**



	Li	Sb	P	As	Bi	Te	Tl	C	Mg	Se	Cr	Ta	Cs	Ba	S	Mn	Ag	Cd	Pt	Si
Si	.033	.039	.045	.054	.069	.14	.21	.25	.25	.25	.4	.41	.43	.3	.32	.26	.2	.25	.34	.14
									.11 A								.36 A	.45 A	.49 A	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14
										.4	.41	.43	.43	.3	.32	.26	.2	.25	.34	.14

Doping in GaAs

For GaAs:

p dopant:

replace Ga: **Mg, Zn, Be**

replace As: **C**

...

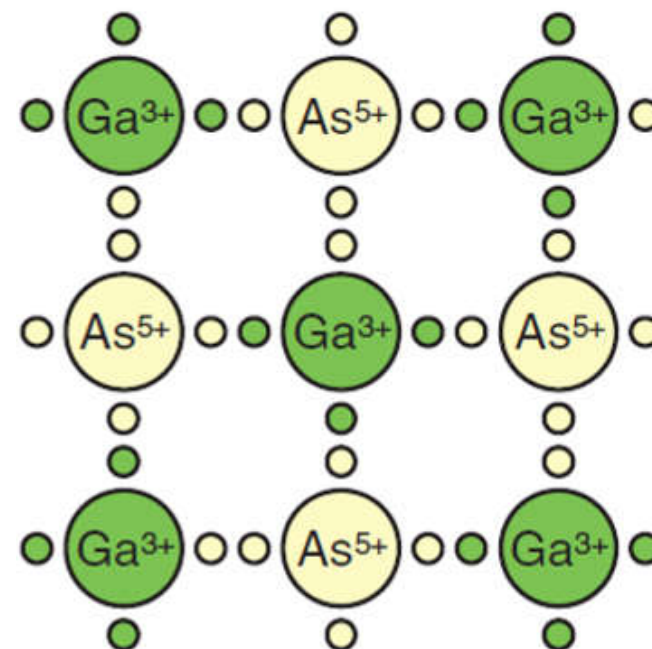
n dopant:

replace As: **Se**

replace Ga: **Si, Ge**

...

					2
	5	6	7	8	9
	B	C	N	O	F
	13	14	15	16	17
	Al	Si	P	S	Cl
	31	32	33	34	35
	Ga	Ge	As	Se	Br
	49	50	51	52	53
	In	Sn	Sb	Te	I
	81	82	83	84	85
	Tl	Pb	Bi	Po	At
					86
					Rn



Doping Methods

- Thermal diffusion 热扩散
- Ion implantation 离子注入
- In situ growth 原位掺杂

Thermal Diffusion - Silicon

Sources

■ Phosphorus (P)

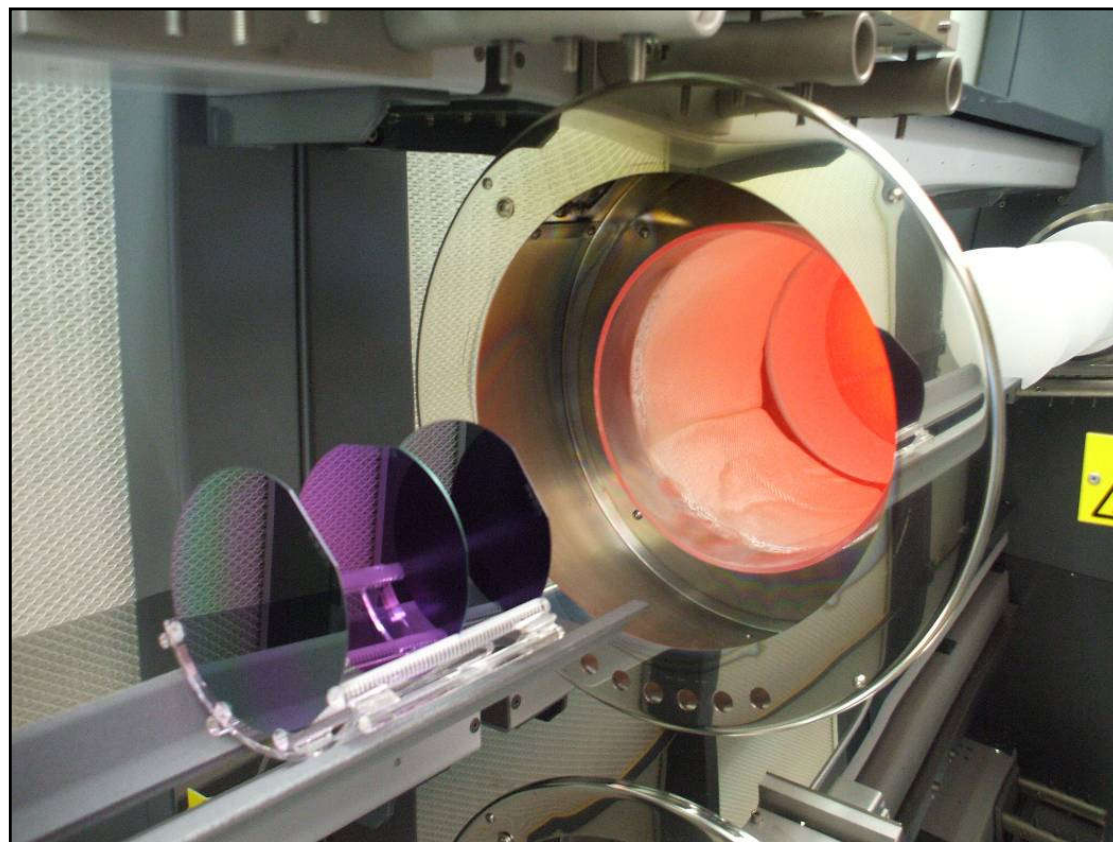
- Liquid - POCl_3
- Gas - PH_3

■ Boron (B)

- Liquid - BBr_3
- Solid - B_2O_3
- Gas - B_2H_6

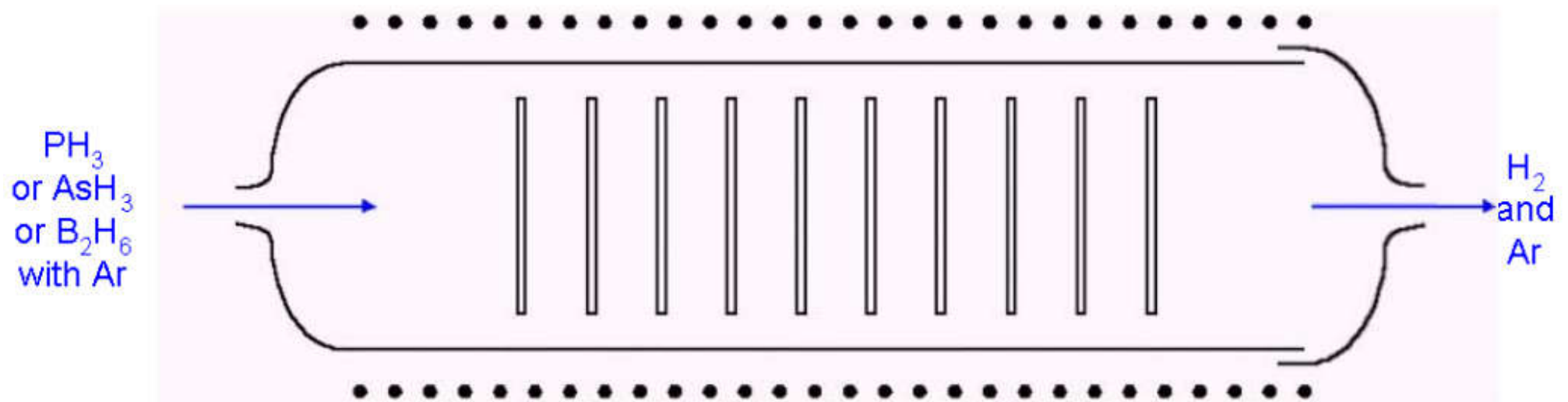
■ Arsenic (As)

- Solid - As_2O_3
- Gas - AsH_3



Thermal Diffusion - Silicon

Gas Source Diffusion



Thermal Diffusion - Silicon

Liquid Source Diffusion

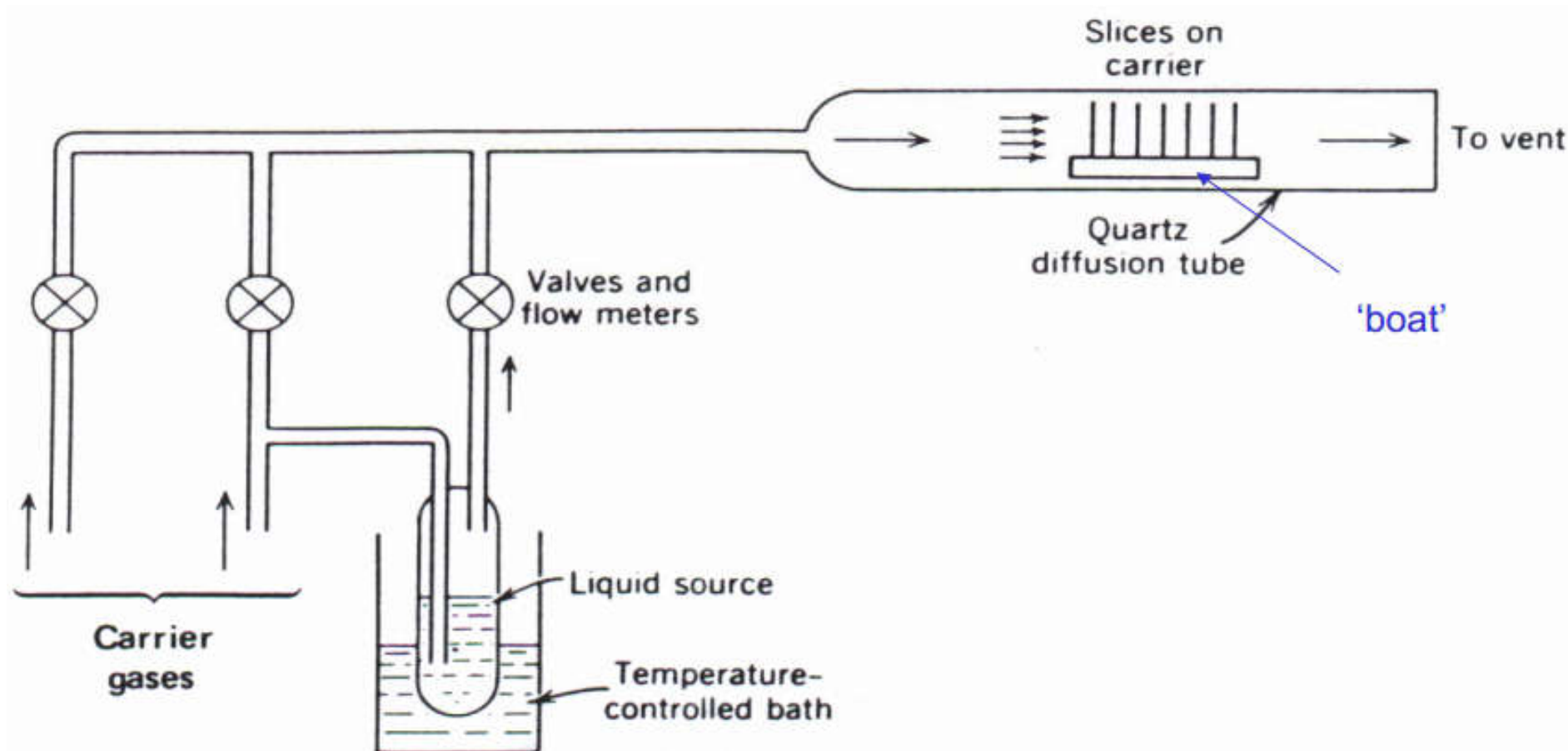


Fig. 4.27 Liquid-source diffusion system.

Thermal Diffusion - Silicon

Solid Source Diffusion

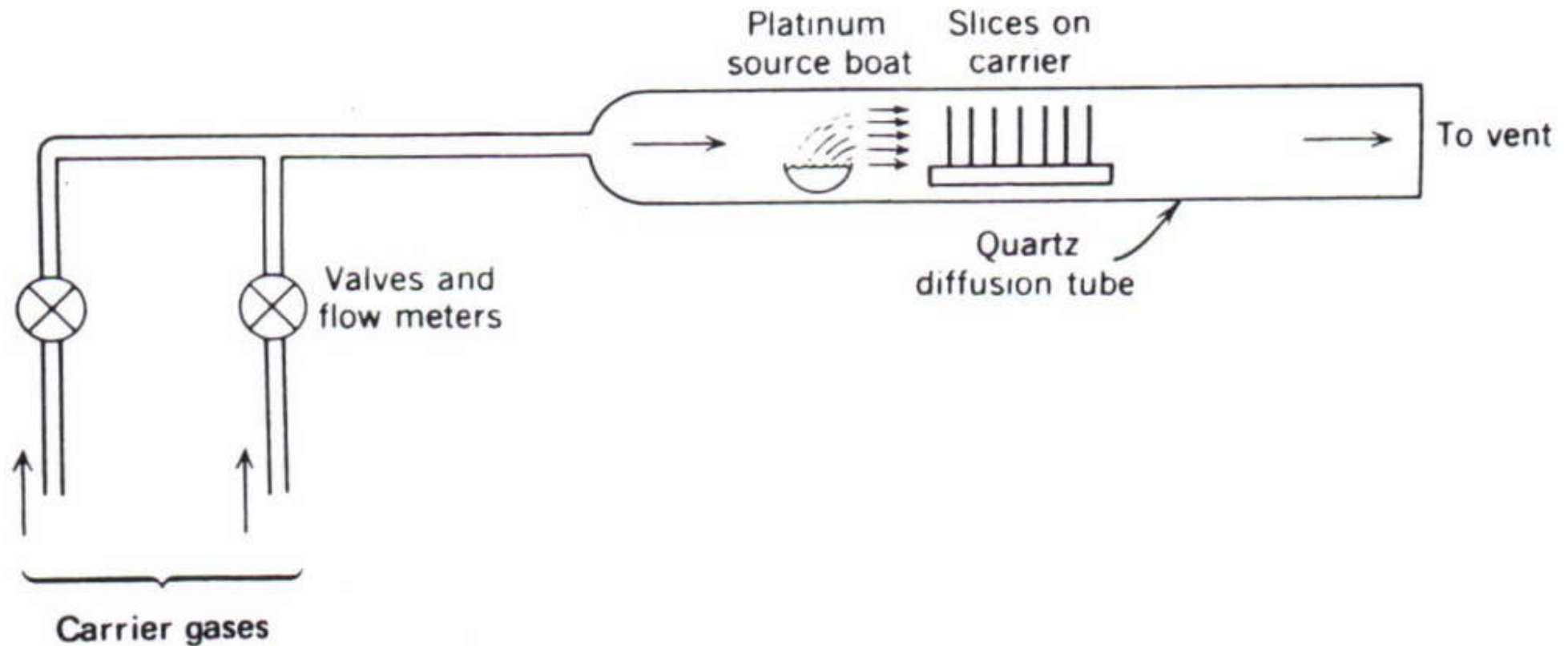
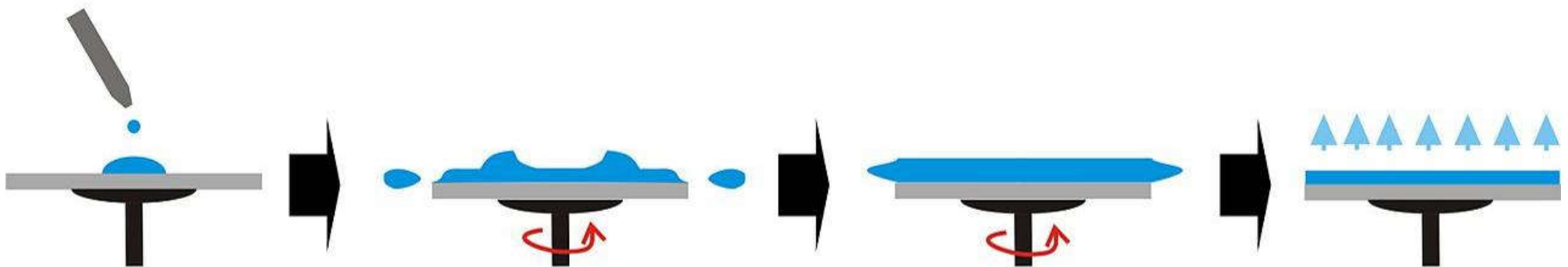
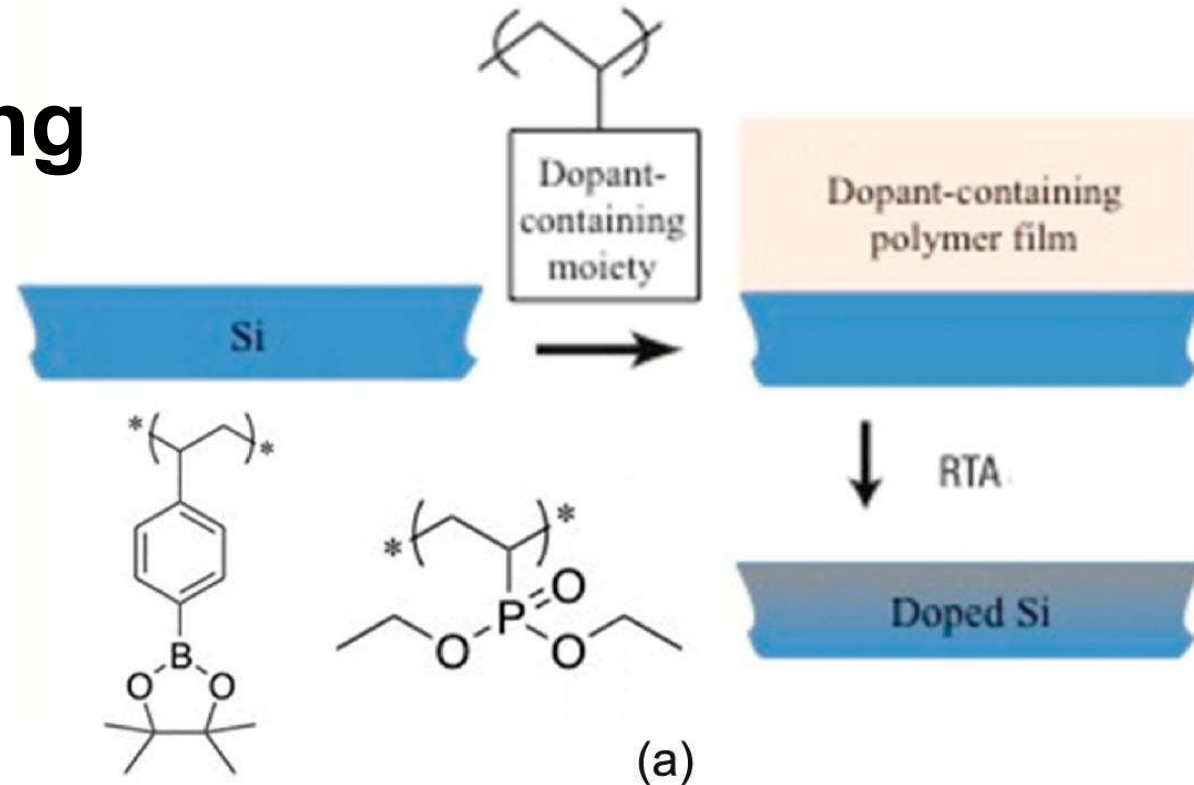


Fig. 4.26 Solid-source diffusion system.

Thermal Diffusion - Silicon

Spin-on doping



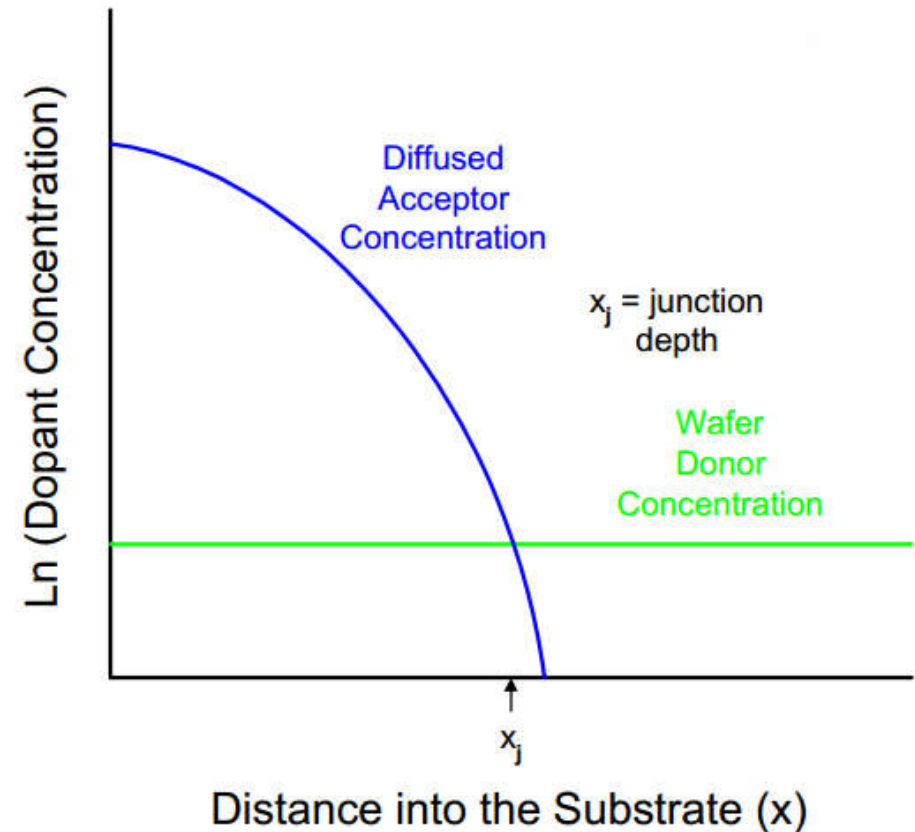
Thermal Diffusion

■ Process Parameters

- Time
- Temperature
- Gas pressure
- Gas flow rate

■ Control Parameters

- Junction depth
- Doping concentration
- Doping profile



Diffusion Law



C concentration (mol/m^3)

$C(x, t)$

J diffusion flux ($\text{mol/m}^2/\text{s}$)

D diffusivity (m^2/s)

Diffusion Law

- Fick's first law

$$\mathbf{1D} \quad J = -D \frac{\partial C}{\partial x}$$

$$\mathbf{3D} \quad \mathbf{J} = -\mathbf{D} \nabla C$$

- Fick's second law

$$\mathbf{1D} \quad \frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial x^2}$$

$$\mathbf{3D} \quad \frac{\partial \mathbf{C}}{\partial t} = \mathbf{D} \nabla^2 \mathbf{C}$$

J : mol/m²/s

D : m²/s

C : mol/m³

Dopant Diffusivity in Silicon

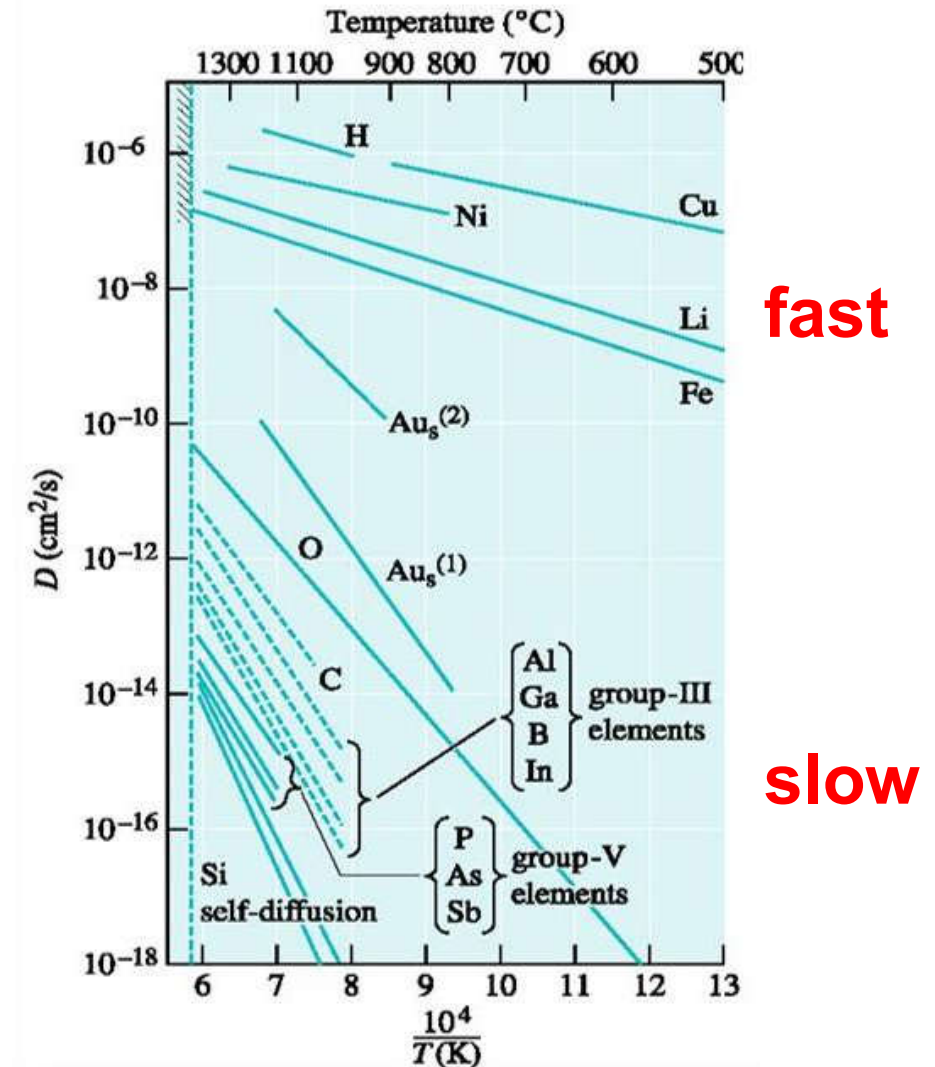
■ Diffusivity (扩散系数) D

- rate of spread
- unit: cm^2/s

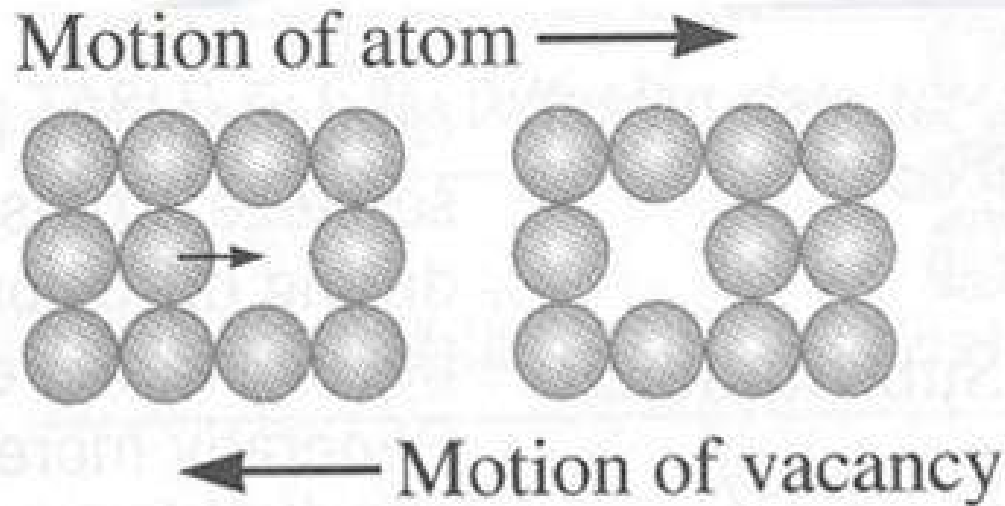
$$D = D_0 \exp\left(-\frac{E_A}{kT}\right)$$

■ Diffusion length L

$$L = \sqrt{Dt}$$

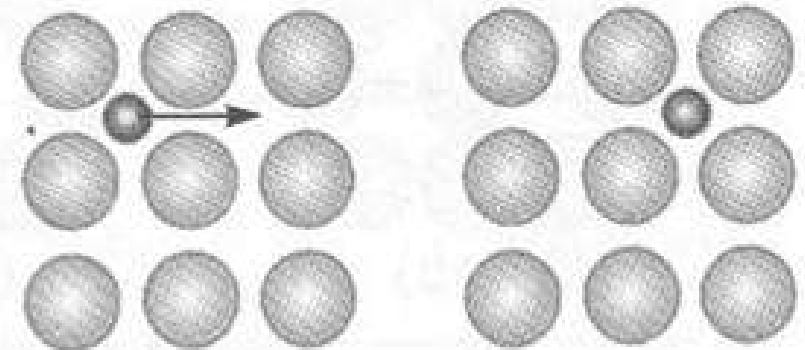


Dopant Diffusivity in Silicon



(a) Vacancy mechanism

B, P, As, Sb, Si, ...

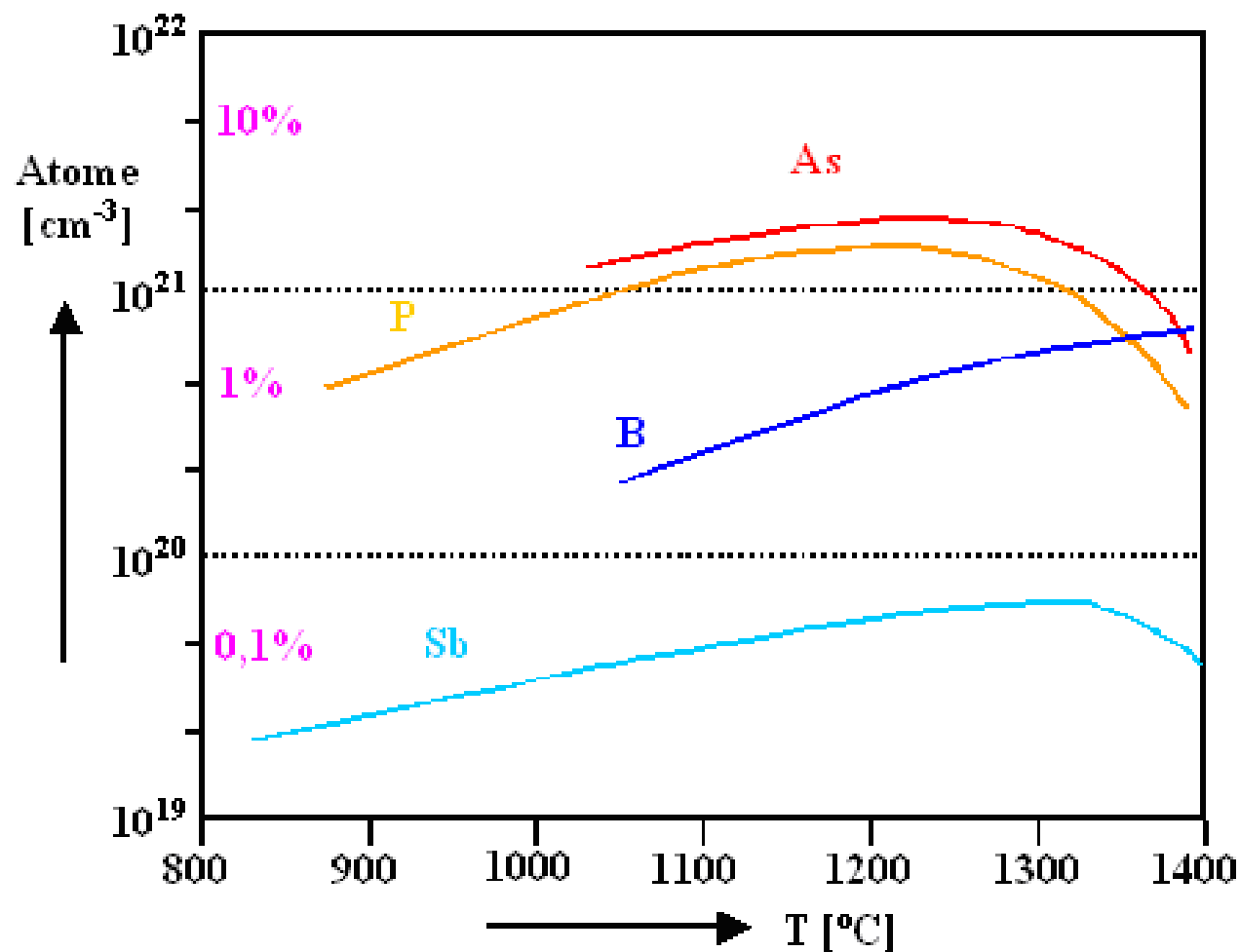


(b) Interstitial mechanism

Cu, Fe, Li, H, Au, ...

Dopant Solubility in Silicon

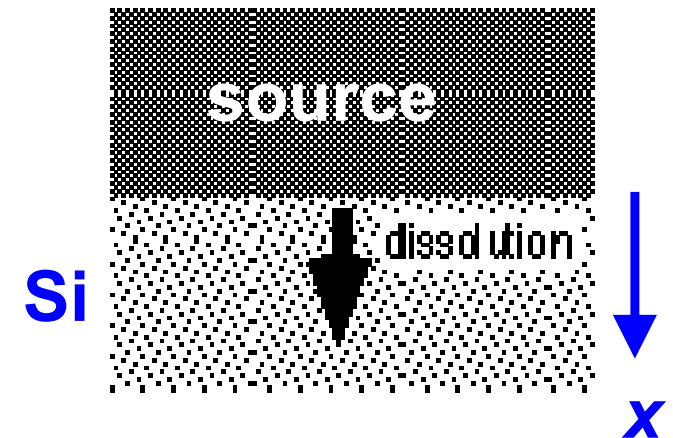
maximum dopant amount in silicon



Dopant Diffusion in Silicon

when the source is semi-infinite,
and the surface is at the solubility limit C_{ss}

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial x^2}$$



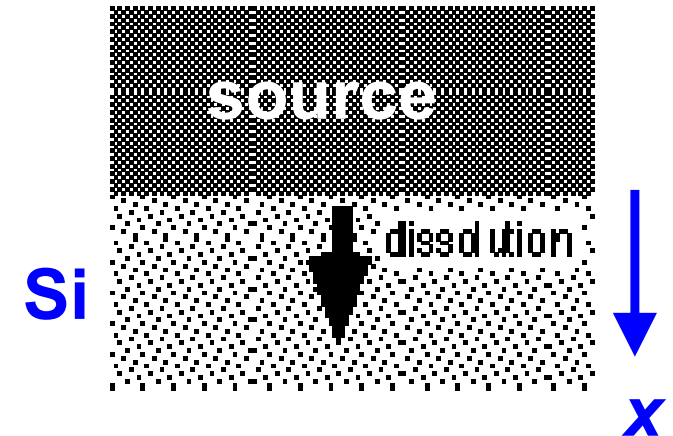
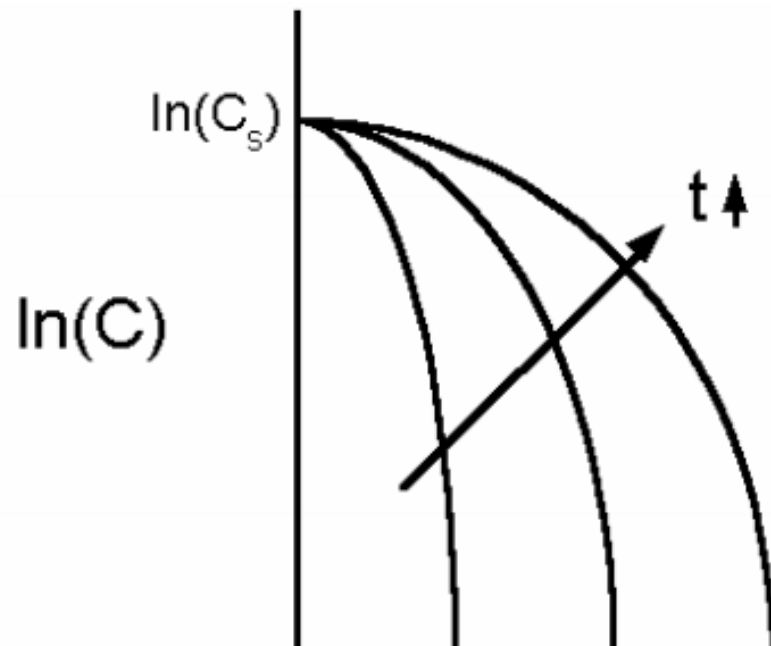
$$\begin{aligned} C(x > 0, t = 0) &= 0 \\ C(x = +\infty, t > 0) &= 0 \\ C(x = 0, t > 0) &= C_{ss} \end{aligned}$$

$$\rightarrow C(x, t) = C_{ss} \cdot \operatorname{erfc}\left(\frac{x}{2\sqrt{Dt}}\right)$$

Error Function

Dopant Diffusion in Silicon

when the source is semi-infinite,
and the surface is at the solubility limit C_{ss}

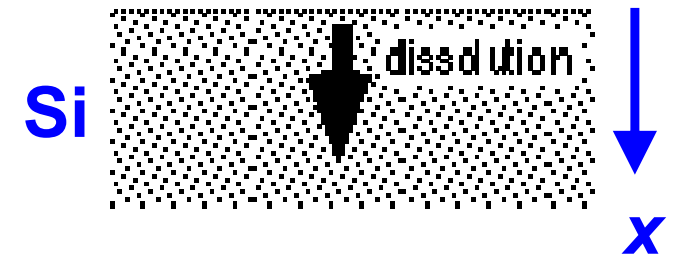


$$C(x, t) = C_{ss} \cdot \operatorname{erfc} \left(\frac{x}{2\sqrt{Dt}} \right)$$

Dopant Diffusion in Silicon

when the source is limited,

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial x^2}$$



$$C(x = 0, t = 0) = Q$$

$$C(x > 0, t = 0) = 0$$

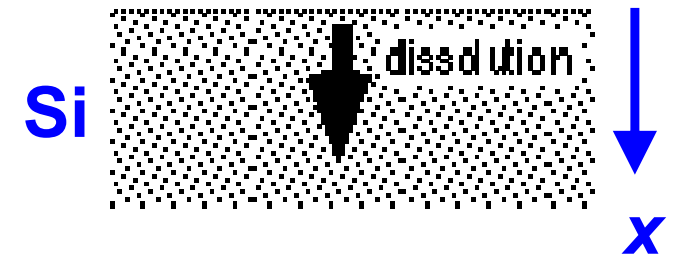
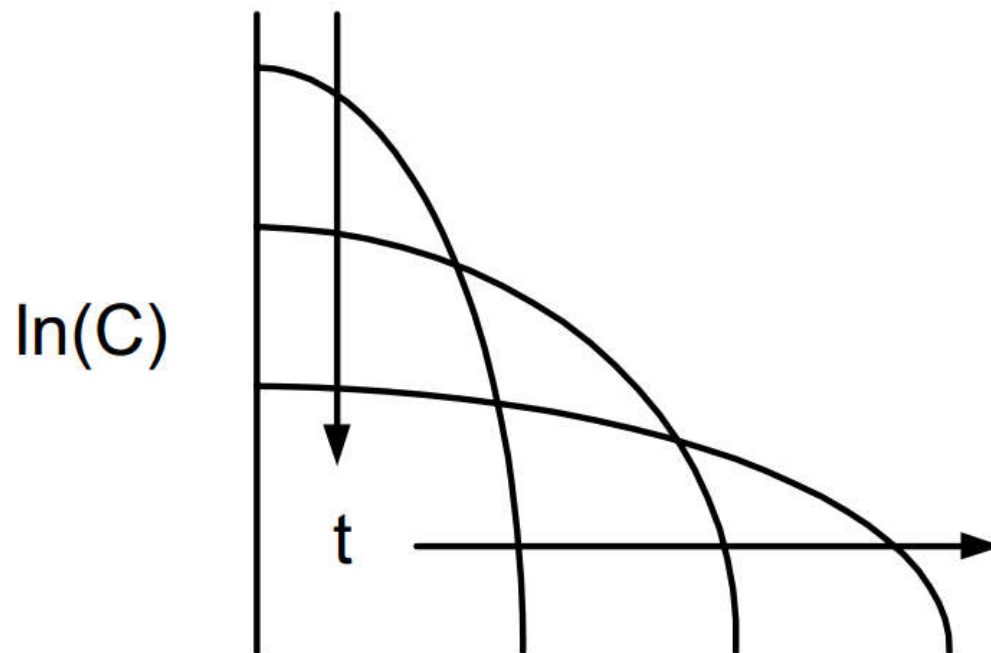
$$C(x = +\infty, t > 0) = 0$$

$$\rightarrow C(x, t) = \frac{Q}{\sqrt{\pi Dt}} \cdot \exp\left(-\frac{x^2}{4Dt}\right)$$

Gaussian Function

Dopant Diffusion in Silicon

when the source is limited,



$$C(x, t) = \frac{Q}{\sqrt{\pi Dt}} \cdot \exp\left(-\frac{x^2}{4Dt}\right)$$

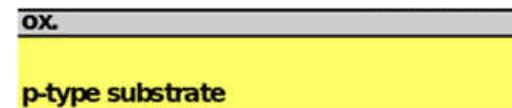
Gaussian Function

Diffusion Masks

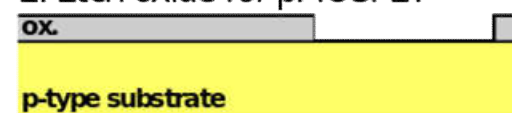
SiO_2 can provide a selective mask against diffusion at high temperatures. ($D_{\text{SiO}_2} \ll D_{\text{Si}}$)
Oxides used for masking are $\sim 0.5\text{-}1\mu\text{m}$ thick.

Dopants	Diffusion Constants at 1100 °C (cm^2/s)
B	$3.4 \times 10^{-17} - 2.0 \times 10^{-14}$
Ga	5.3×10^{-11} (not good for Ga)
P	$2.9 \times 10^{-16} - 2.0 \times 10^{-13}$
As	$1.2 \times 10^{-16} - 3.5 \times 10^{-15}$
Sb	9.9×10^{-17}

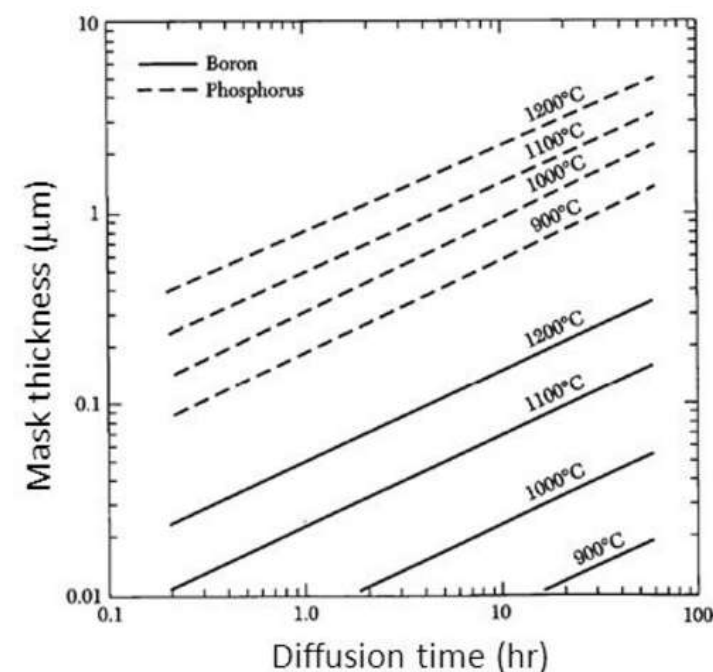
1. Grow field oxide



2. Etch oxide for pMOSFET

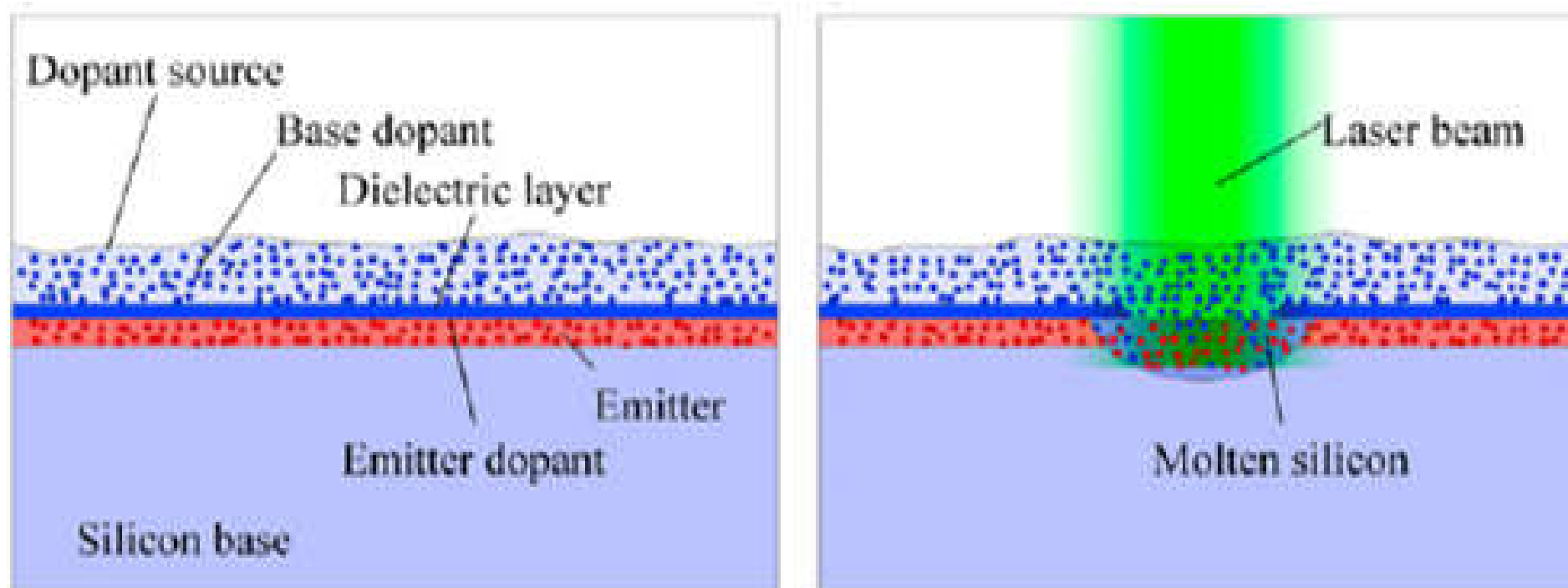


3. Diffuse n-well



Q: why not photoresist?

Laser Assisted Annealing

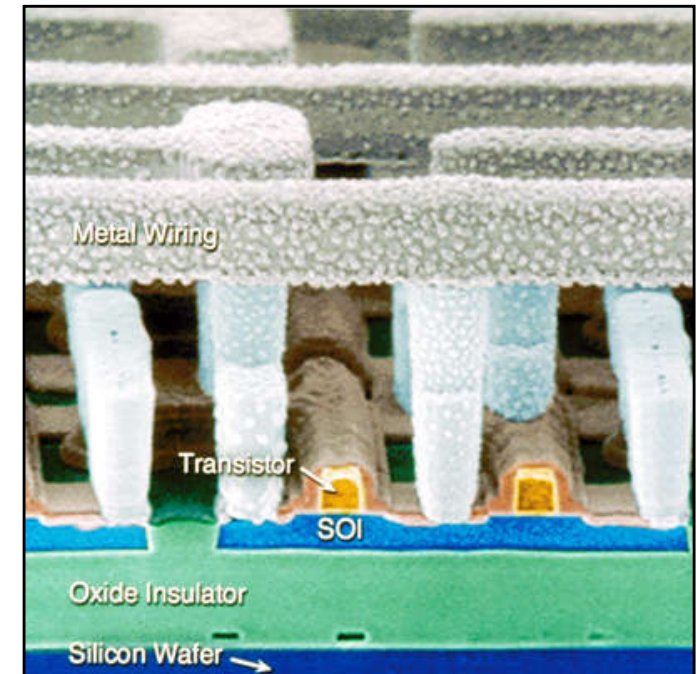


local heating

Doping in Nano Devices

*atomic density of Si = $5 * 10^{22} / \text{cm}^3$*

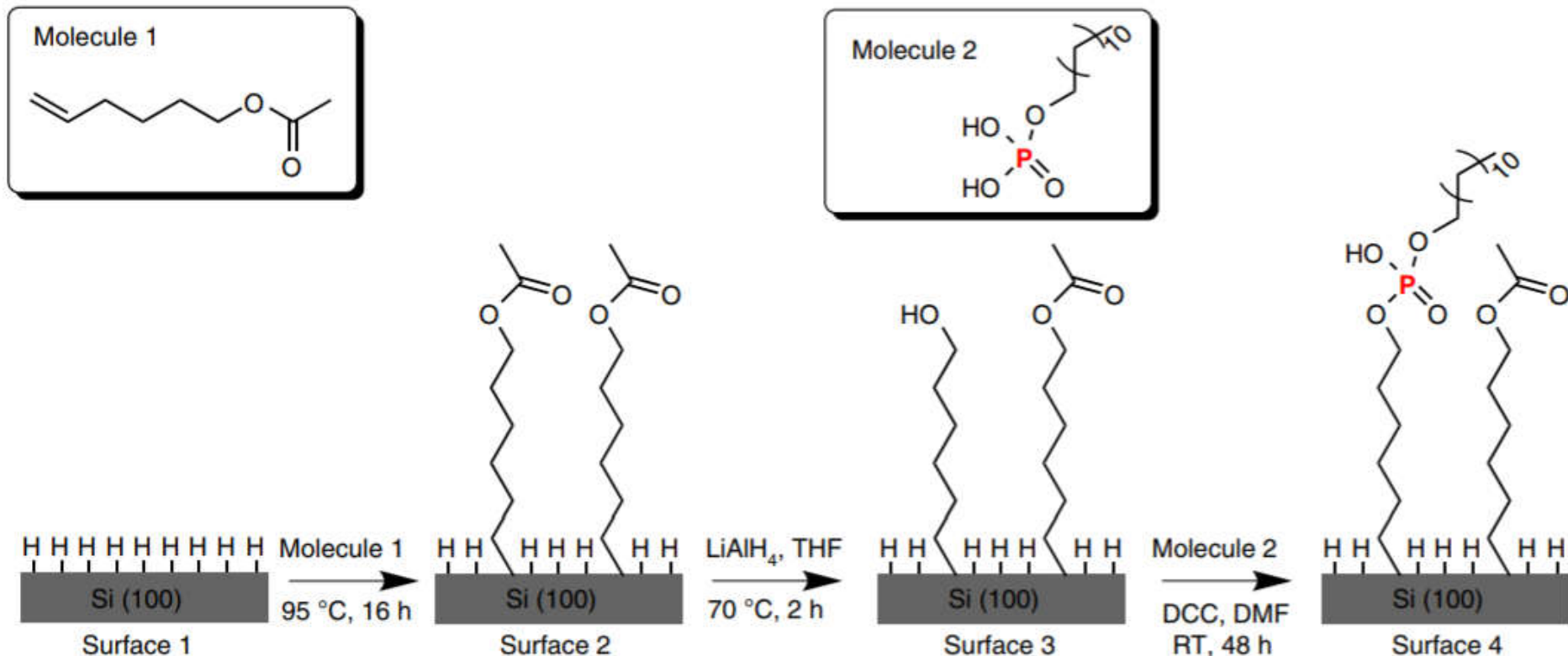
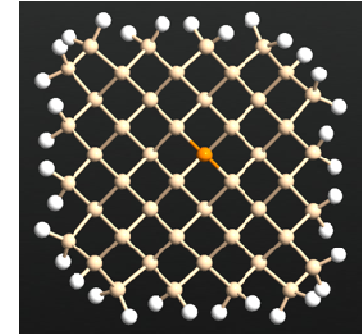
if the transistor size is
 $10 \text{ nm} * 10 \text{ nm} * 10 \text{ nm}$,
and doping concentration is
 $1 * 10^{18} / \text{cm}^3$



There is only 1 dopant atom in the transistor!

Single Atom Doping

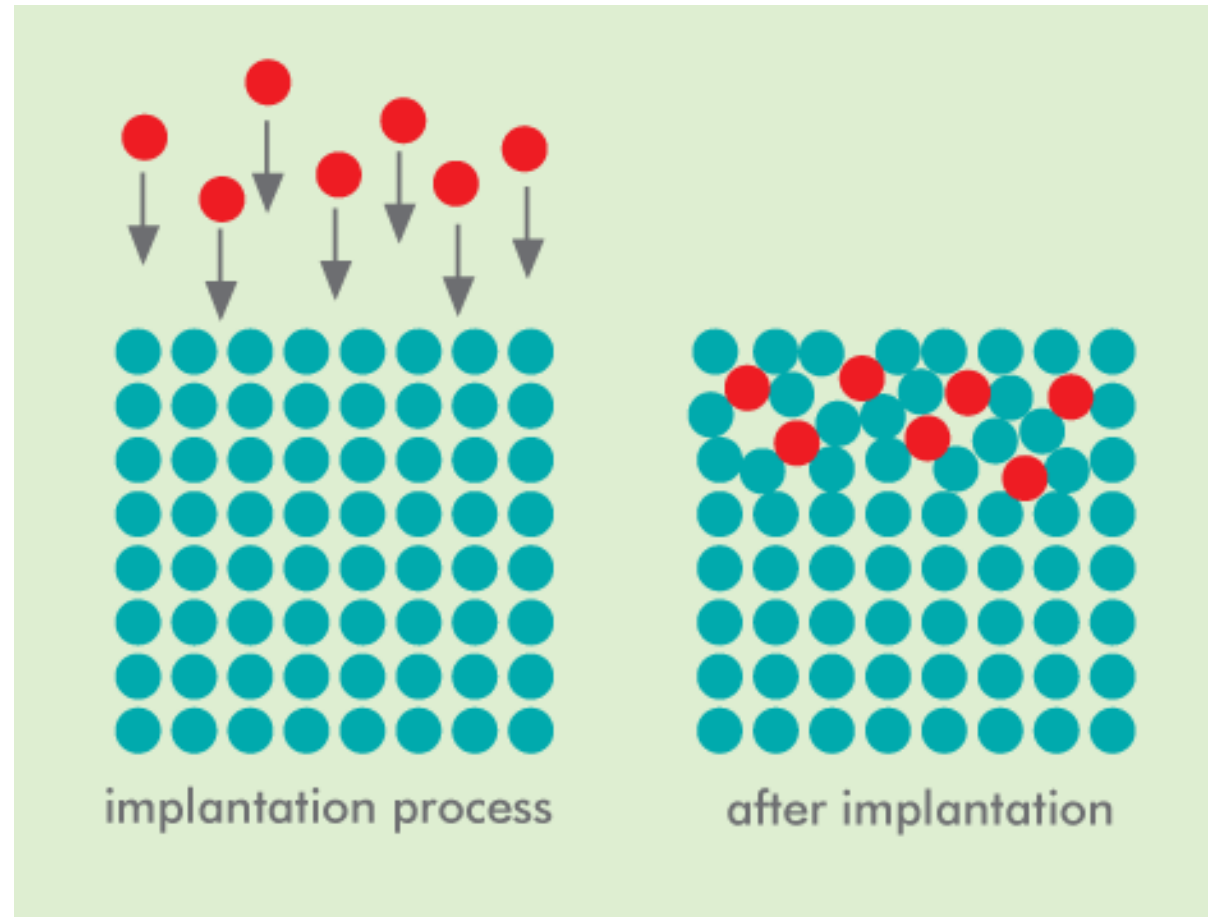
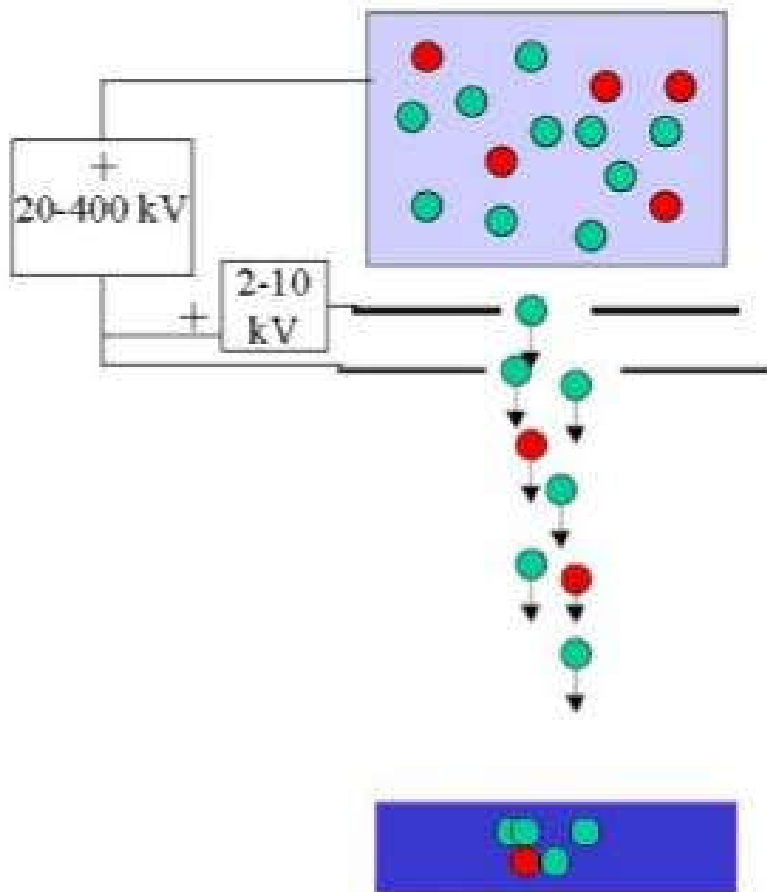
The dopant is provided by *self-assembled molecular monolayers*



Doping Methods

- Thermal diffusion 热扩散
- Ion implantation 离子注入
- In situ growth 原位掺杂

Ion Implantation (离子注入)



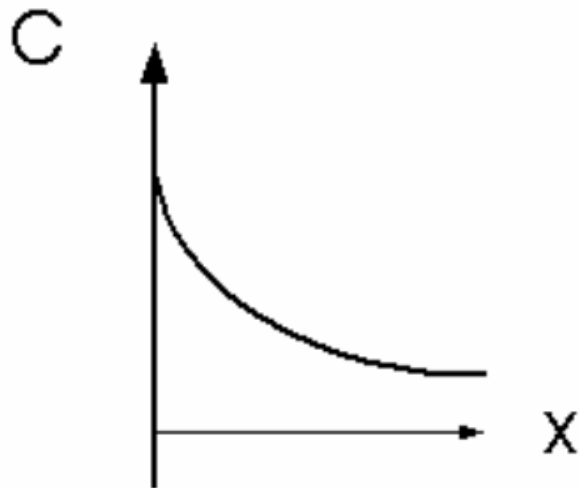
[Video](#)

Ion Implantation - Advantages

- **Precise control of dose, depth and profile**
- **Low temperature process**
- **Tailor lateral distribution**
- **Wide selection of dopants**

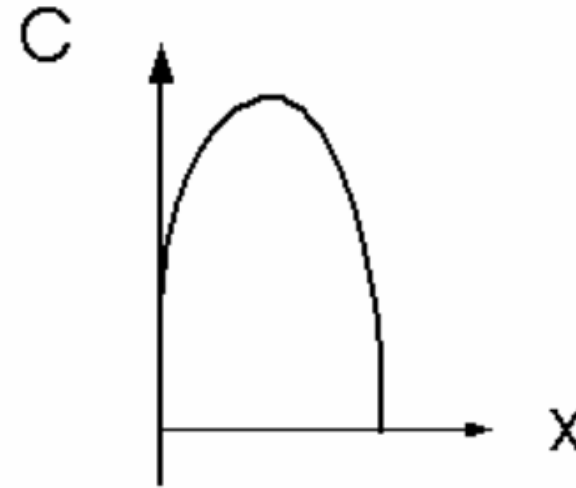
Ion Implantation - Advantages

- Precise control of dose, depth and profile



Thermal diffusion

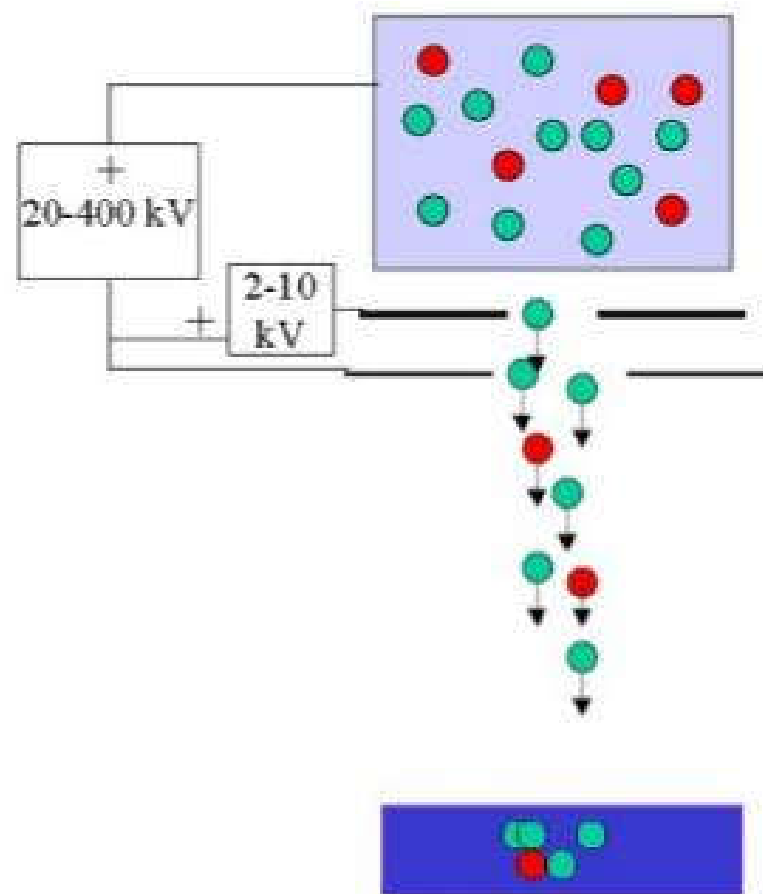
vs.



Ion implantation

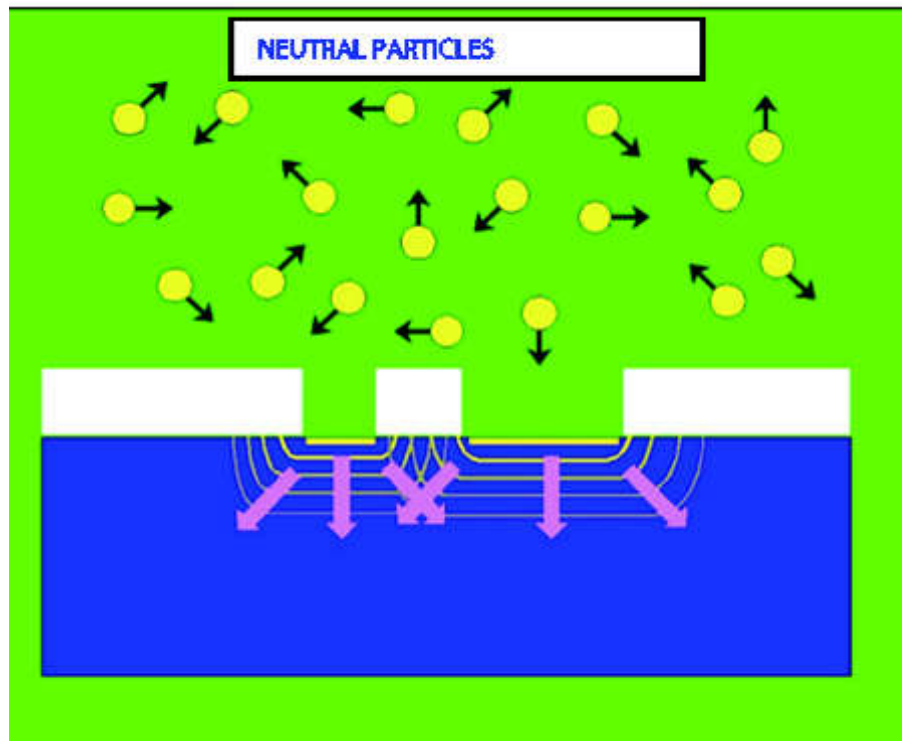
Ion Implantation - Advantages

- **Low temperature process**
 - **implantation at room temperature**
 - **mask materials: photoresist, SiO₂, metal, ...**

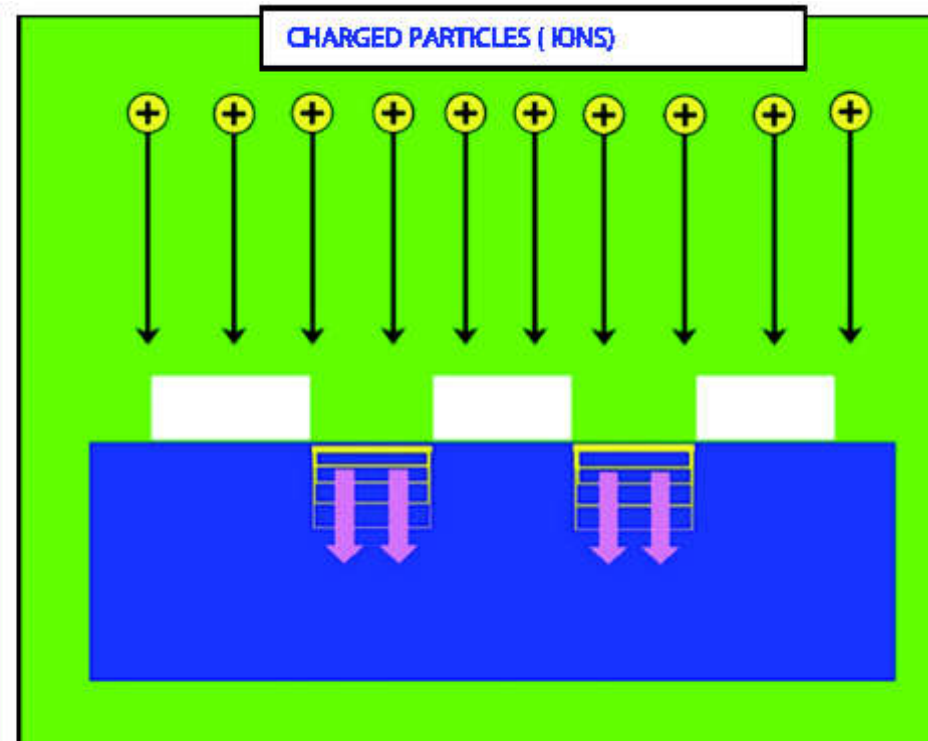


Ion Implantation - Advantages

- Lateral distribution



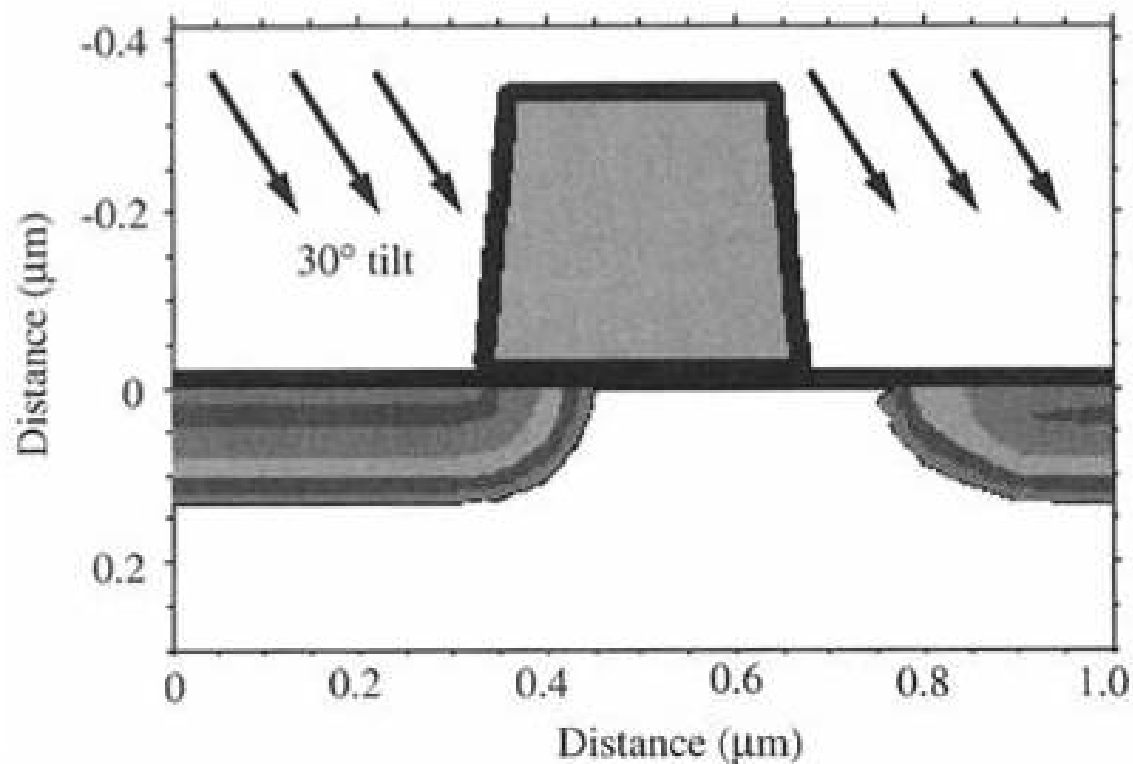
Thermal diffusion



Ion implantation

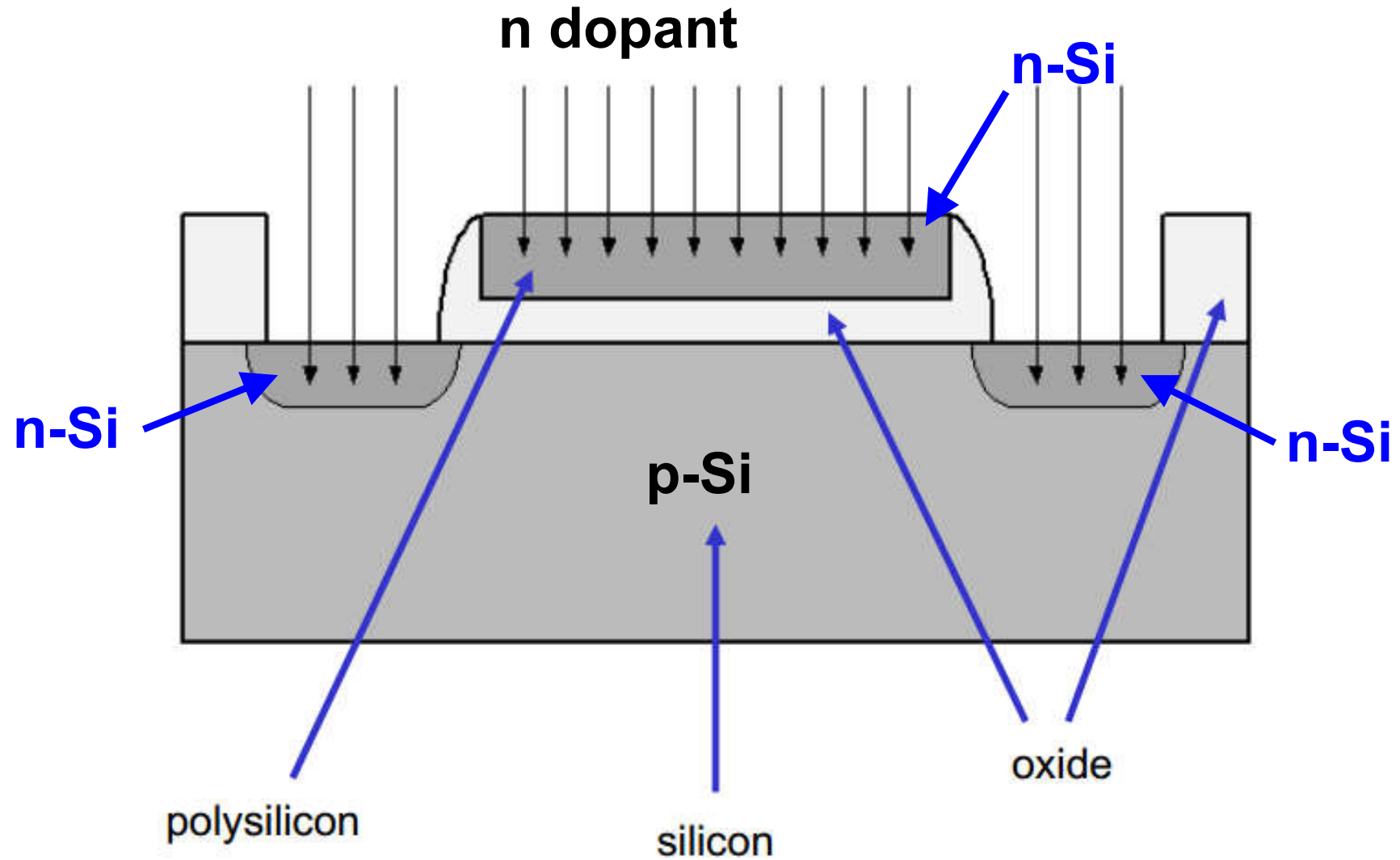
Ion Implantation - Advantages

- Lateral distribution



shadow effect

Self Alignment



Dopant Distribution

■ Process Parameters

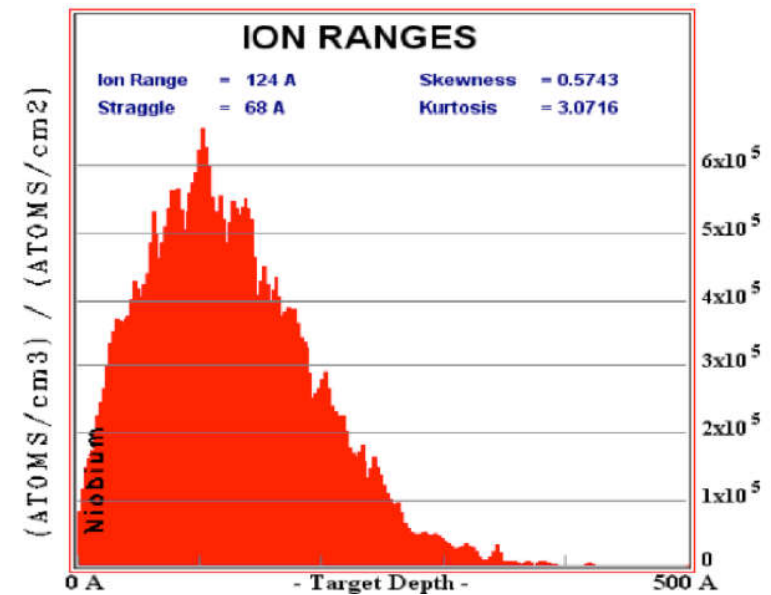
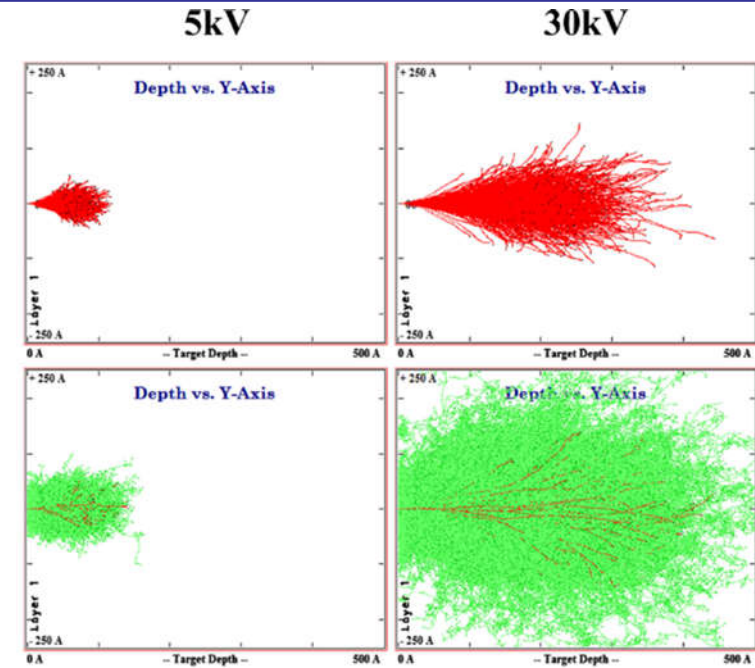
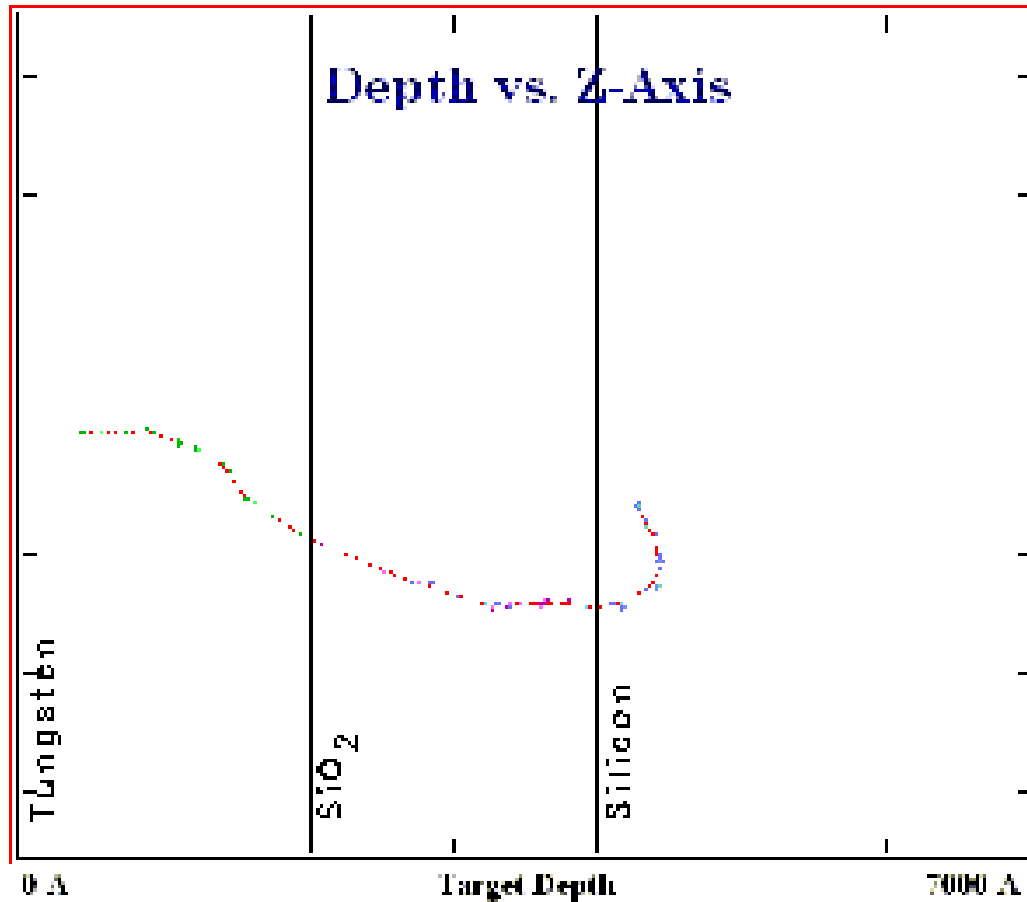
- ❑ dopant type (B, P, As, Sb, ...)
- ❑ implantation dose ($\#/cm^2$)
- ❑ energy (eV)
- ❑ substrate orientation
- ❑ anneal time
- ❑ anneal temperature

■ Control Parameters

- ❑ Junction depth
- ❑ Doping concentration
- ❑ Doping profile

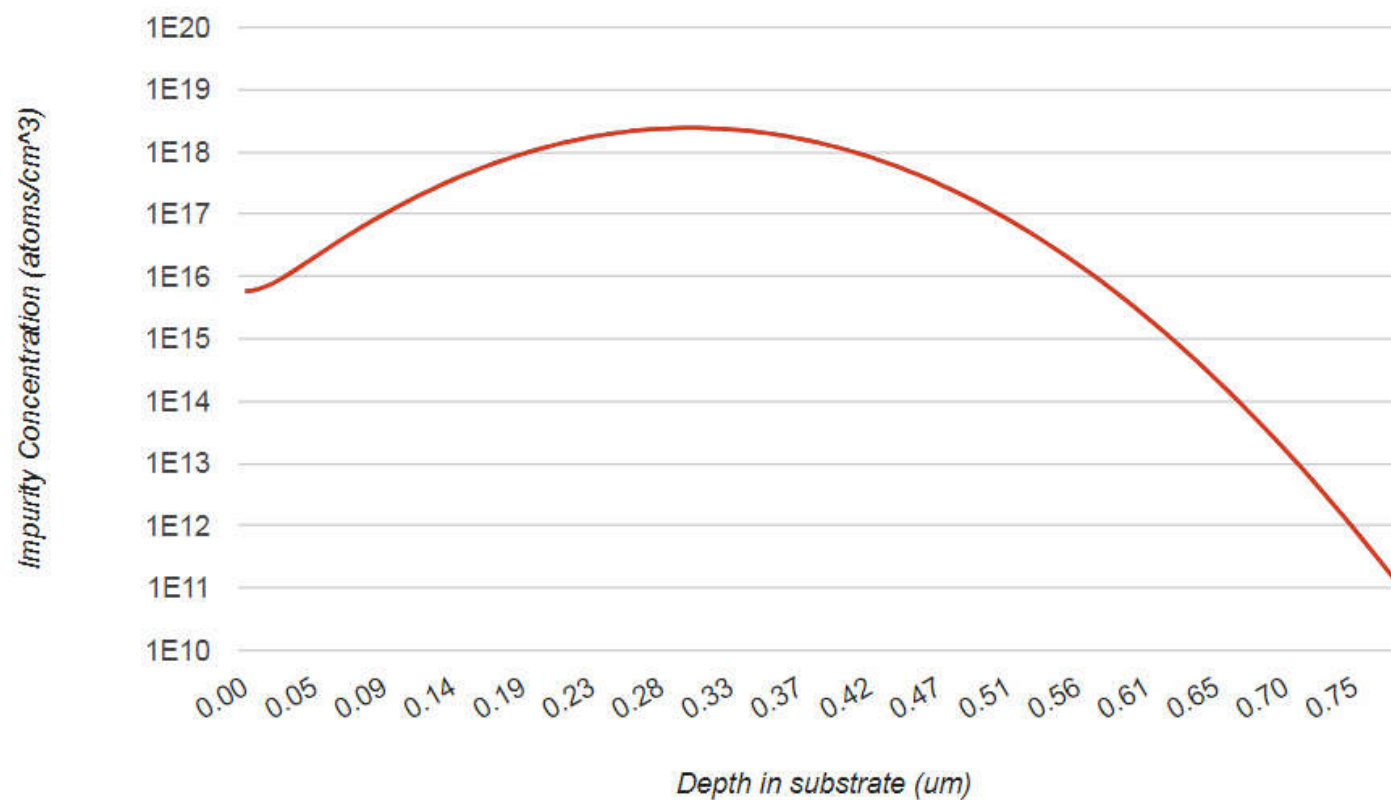
Simulation Software - SRIM

<http://www.srim.org>



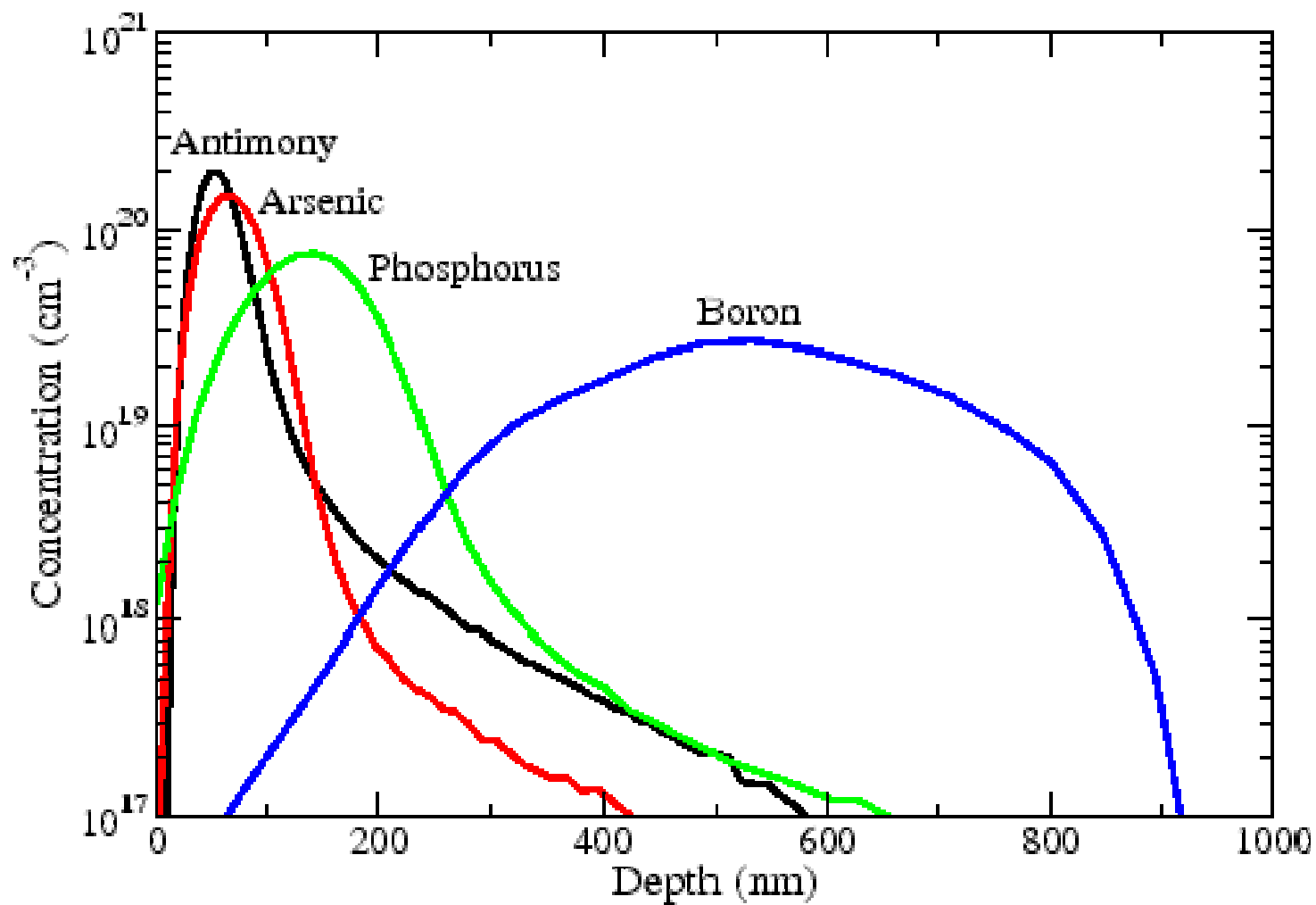
Simulation Website

Dopant: <input type="radio"/> Arsenic <input checked="" type="radio"/> Boron <input type="radio"/> Phosphorus	Diffusion Temperature: <input type="text" value="1000"/> [°C]	Diffusion Time: <input type="text" value="10"/> [minutes]	Substrate Depth (x): <input type="text" value="1"/> [μm]
			<input type="button" value="Calculate Concentration"/>
			<input type="button" value="CSV"/>
Implant 1 Ion <input type="text" value="100"/> Energy: <input type="text" value="100"/> [keV] (0-400) Ion Dose: <input type="text" value="1e14"/> [ions/cm ²]	Ion Concentration at x: <input type="text" value="4.089165464949088e2"/> [atoms/cm ³]		



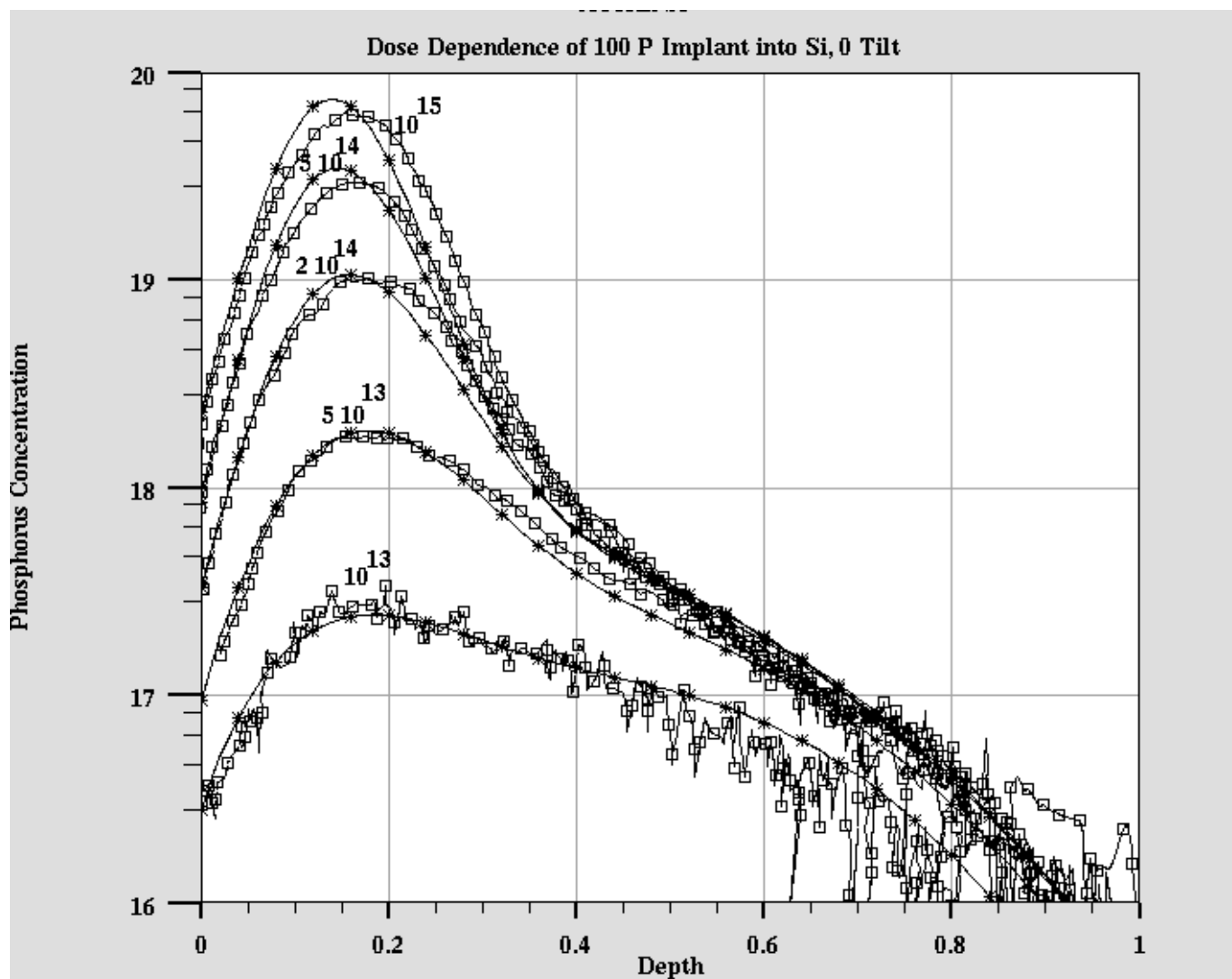
Dopant Distribution

dopant type



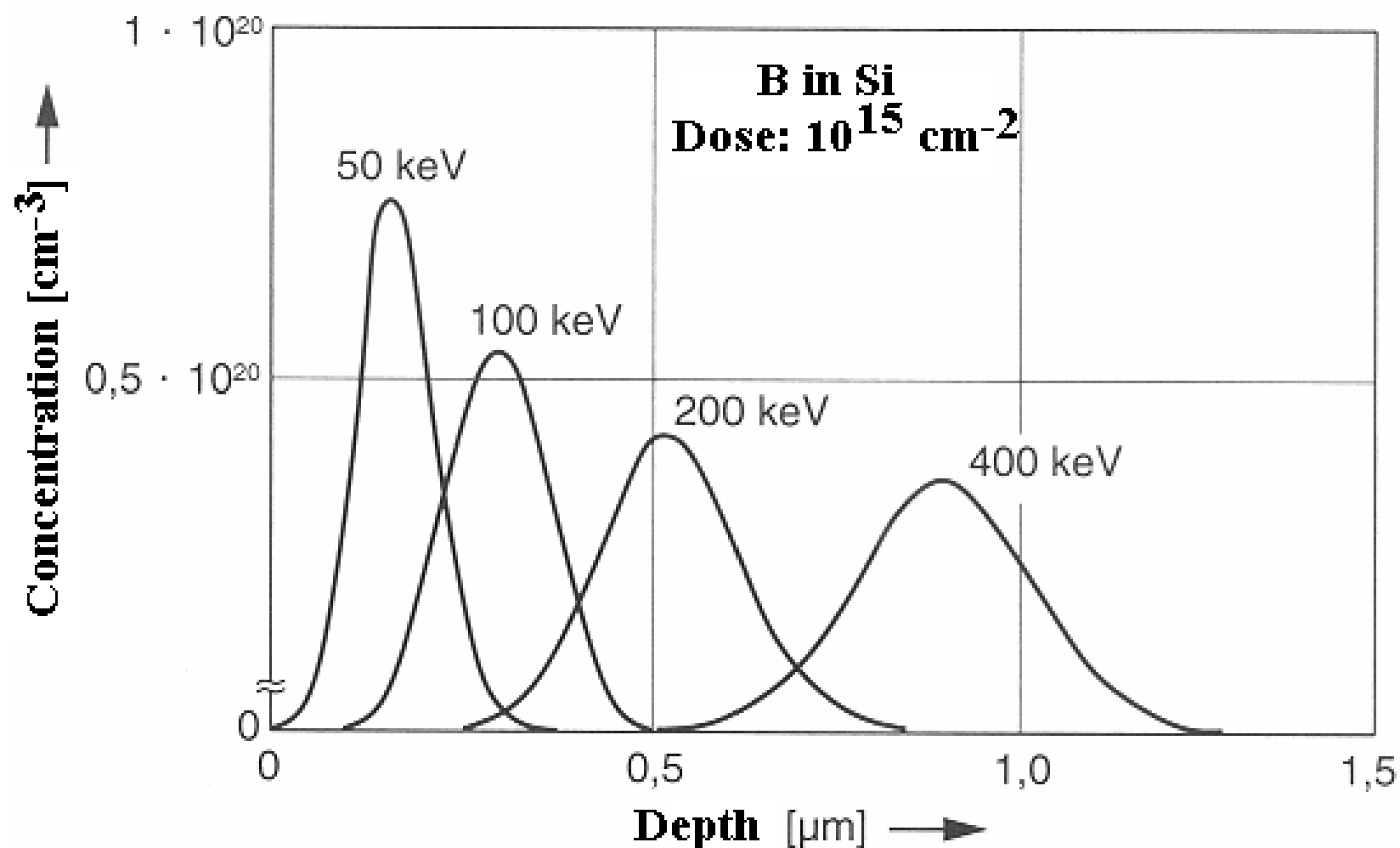
Dopant Distribution

dose



Dopant Distribution

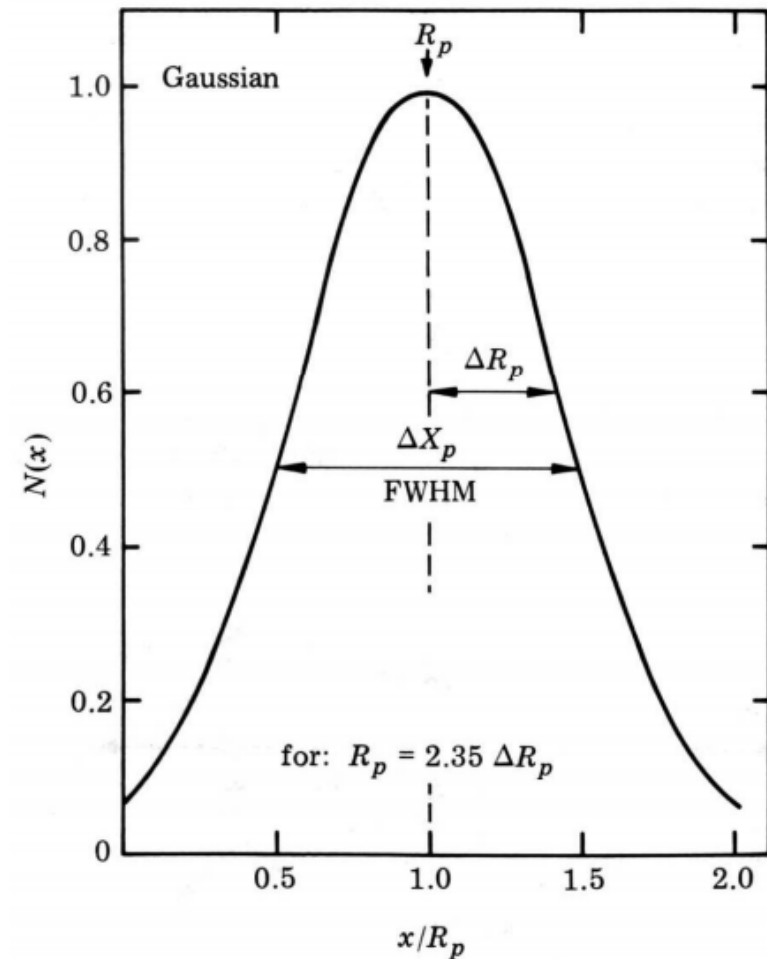
energy



Dopant Distribution

Ideal case: Gaussian profile

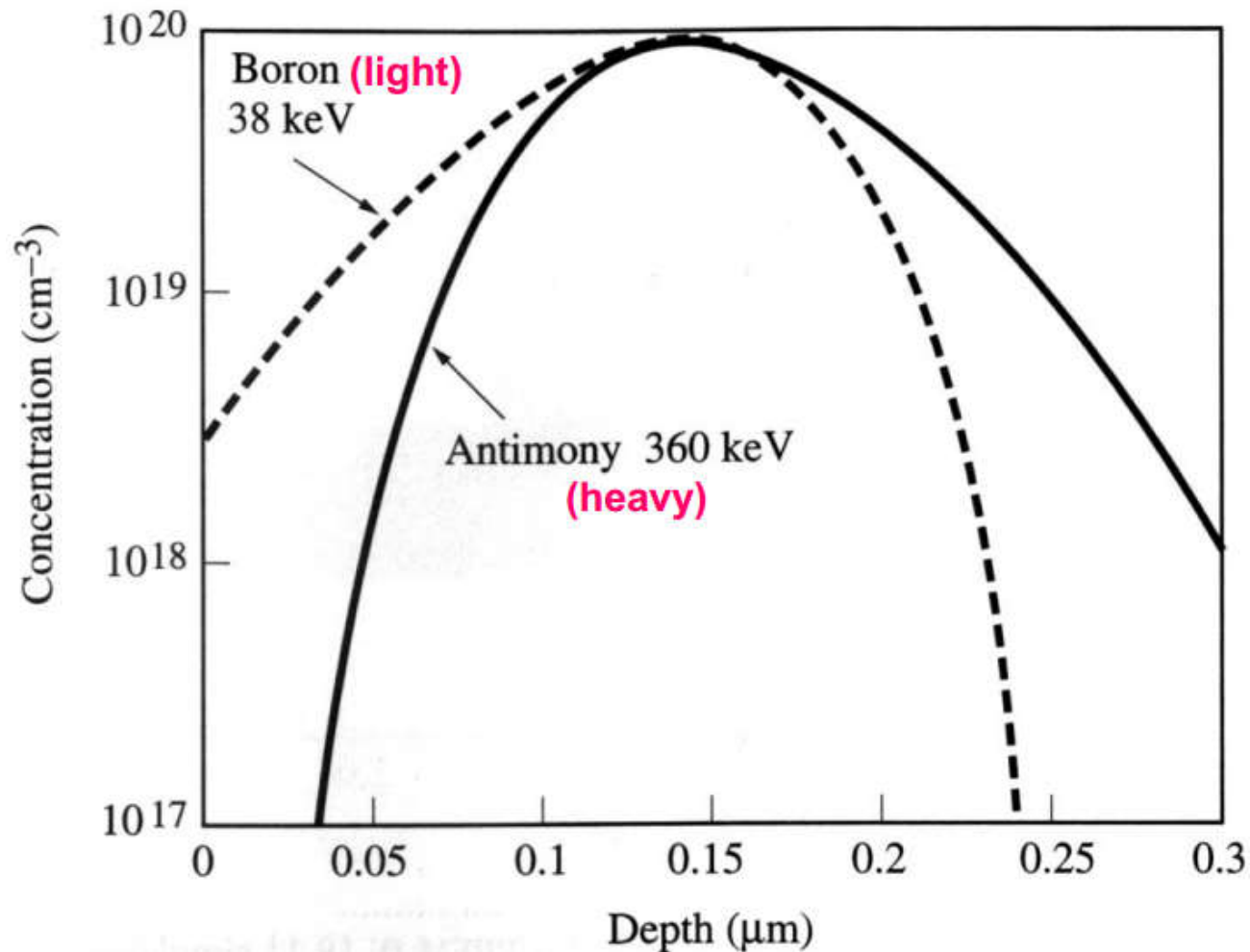
$$C(x) \sim \exp\left[-\frac{1}{2}\left(\frac{x - R_p}{\Delta R_p}\right)^2\right]$$



Dopant Distribution

Light atoms (e.g. B): back scattering

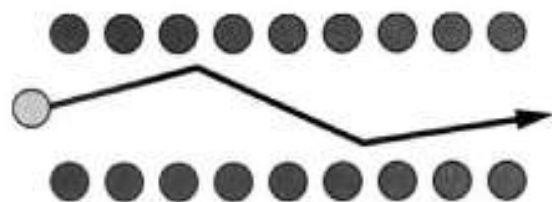
Heavy atoms (e.g. Sb): forward scattering



Dopant Distribution

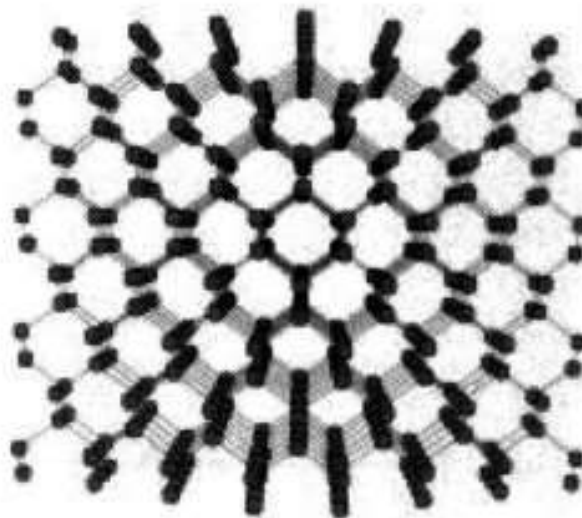
Ion Channeling

(沟道效应)

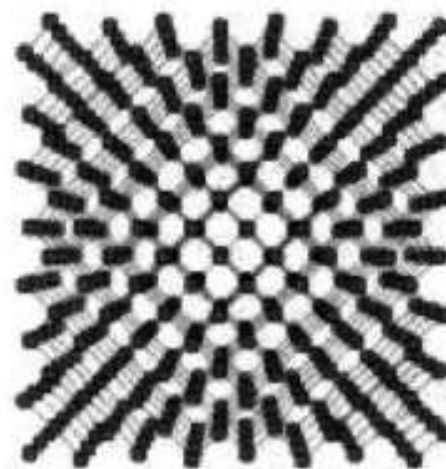
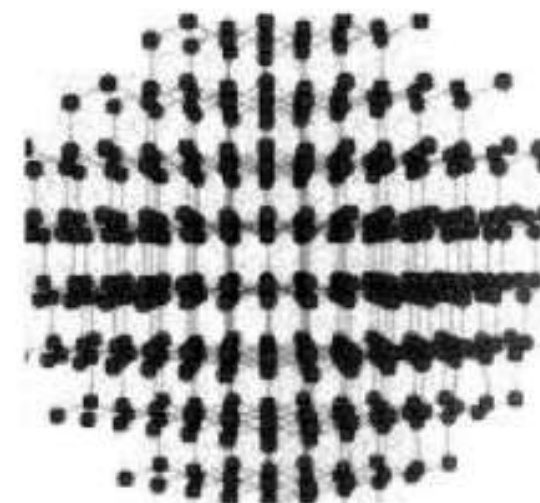


implantation is generally carried out with wafers tilted a few degrees relative to the beam

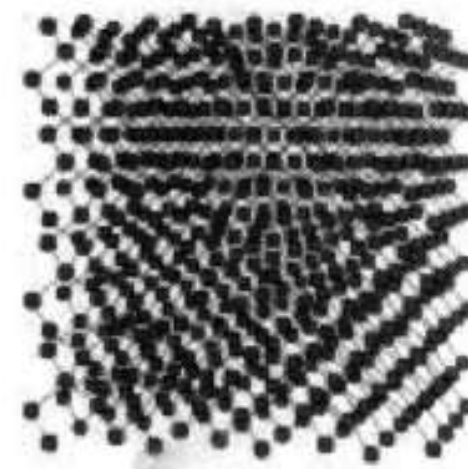
(110) axial



(111) planar

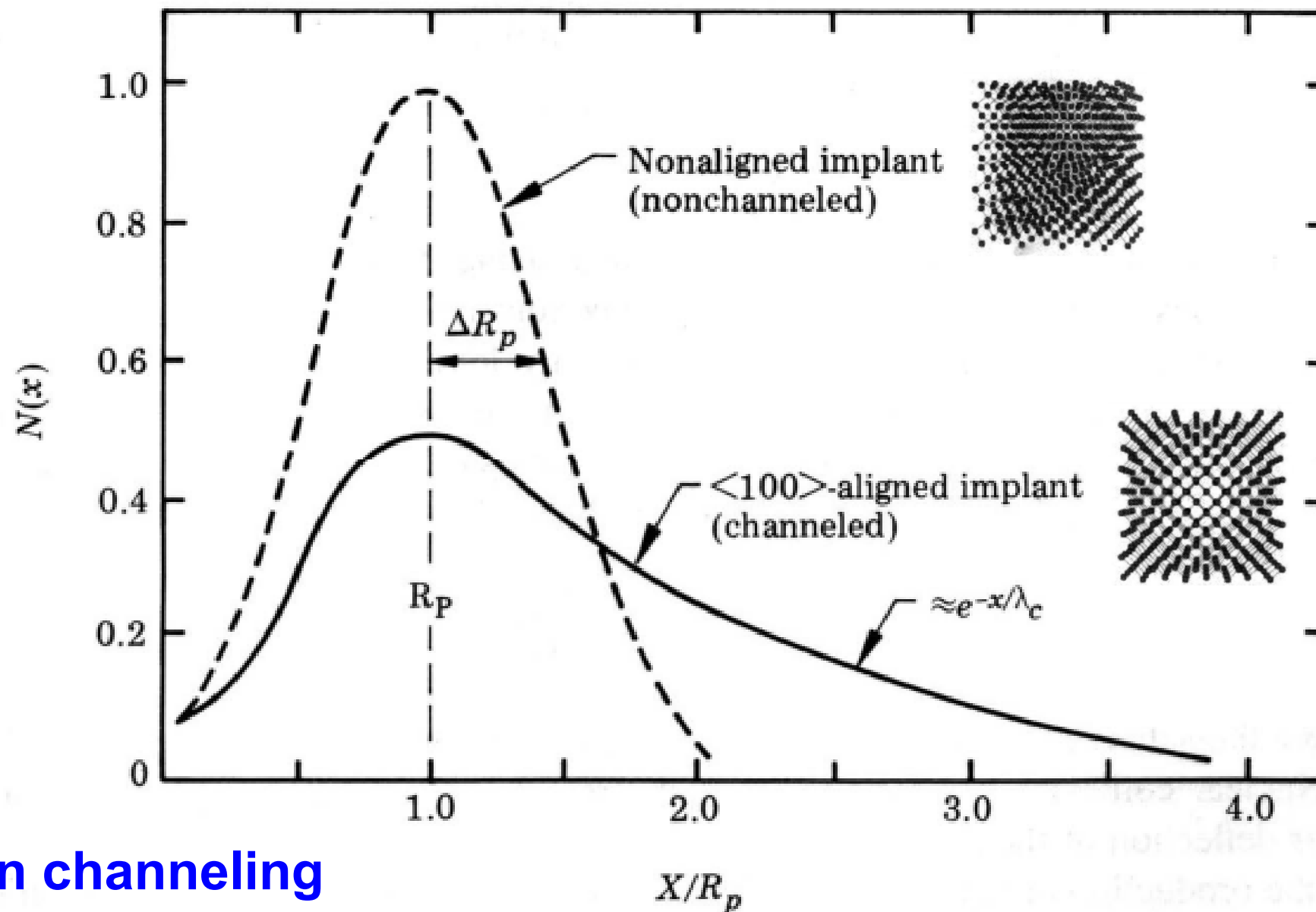


(100) axial



random

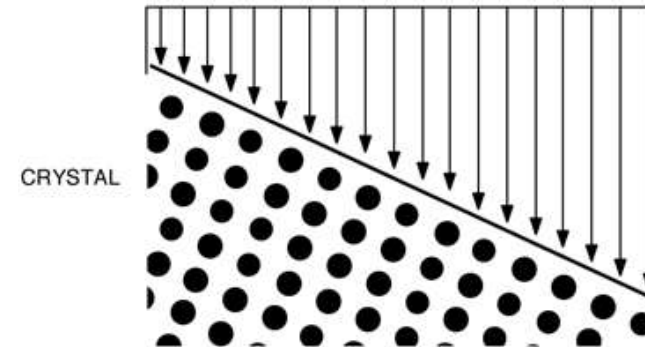
Dopant Distribution



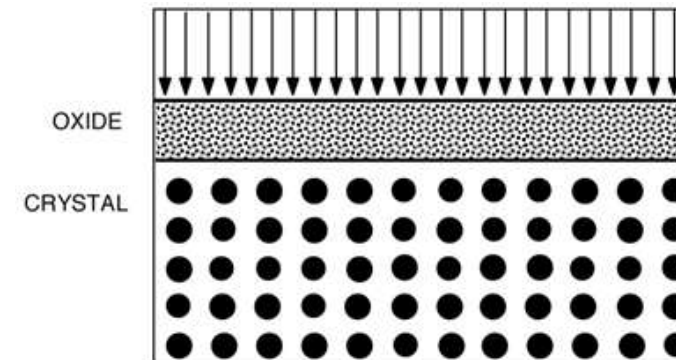
ion channeling

Reduce Channeling Effects

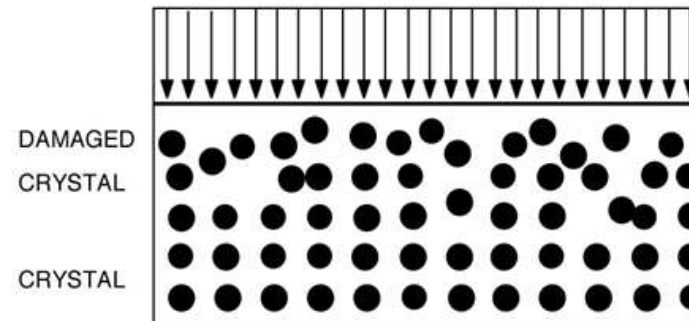
tilt the crystal



form a thin oxide layer

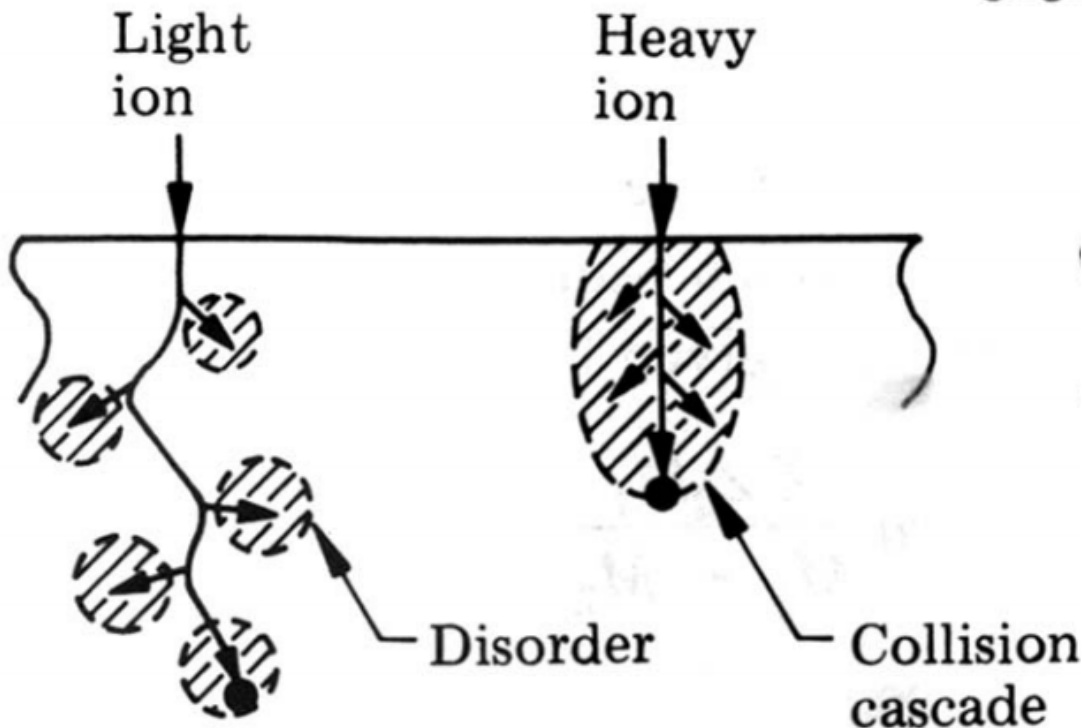
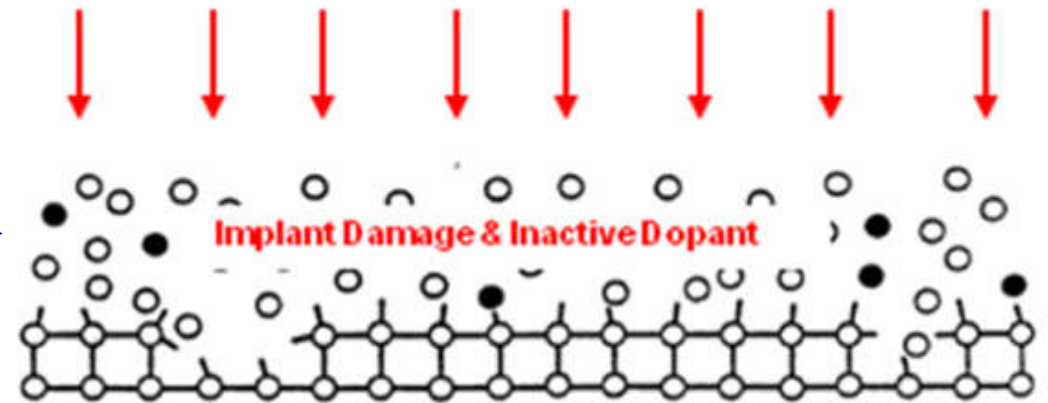


damage the surface
by implantation



Implantation Damage

amorphous →



[Video: Bullet in gel](#)

Implantation Damage

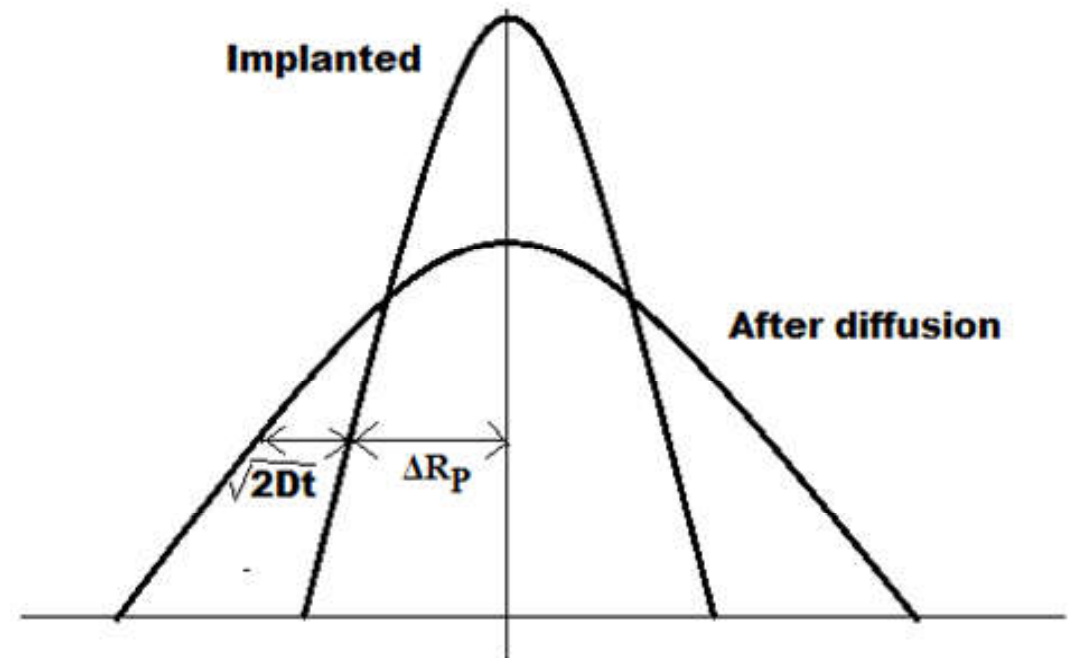
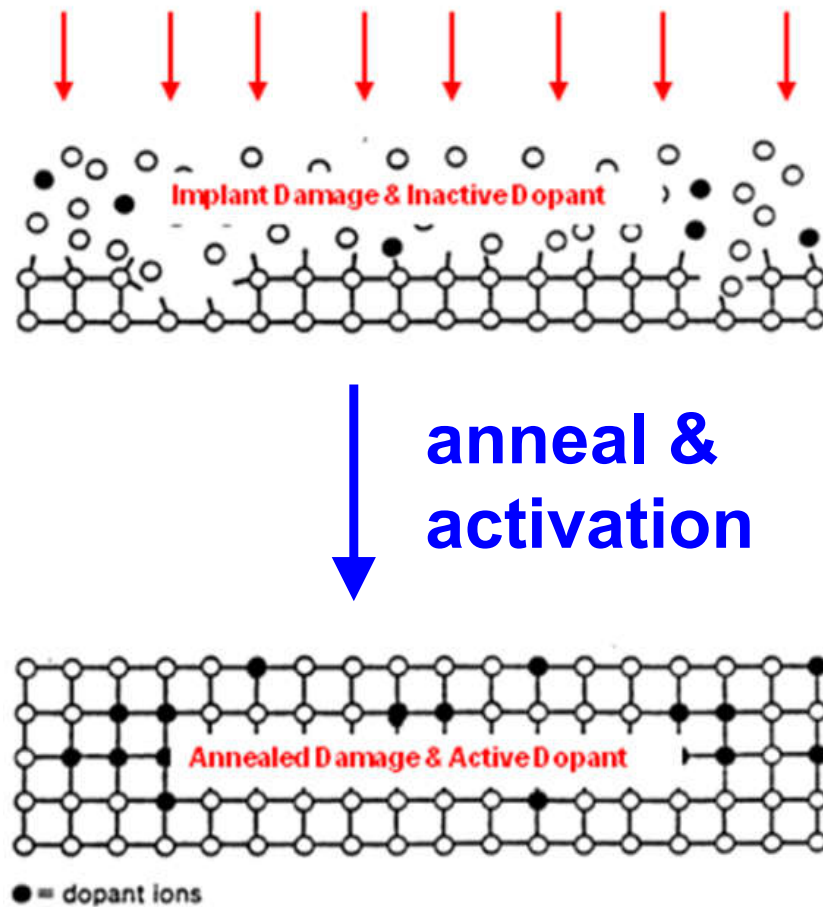


Figure 6.43 Evolution of Gaussian profile after annealing. The Gaussian preserves its shape as it diffuses in an infinite medium.

Effect of Annealing

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial x^2}$$

$$C(x, t = 0) = C_0(x)$$

$$C(x = +\infty, t > 0) = 0$$



$$C(x, t) = \frac{Q}{\sqrt{2\pi(\Delta R_p^2 + 2Dt)}} \cdot \exp\left[-\frac{(x - R_p)^2}{2(\Delta R_p^2 + 2Dt)}\right]$$

$$C_0(x) \sim \exp\left[-\frac{1}{2}\left(\frac{x - R_p}{\Delta R_p}\right)^2\right]$$

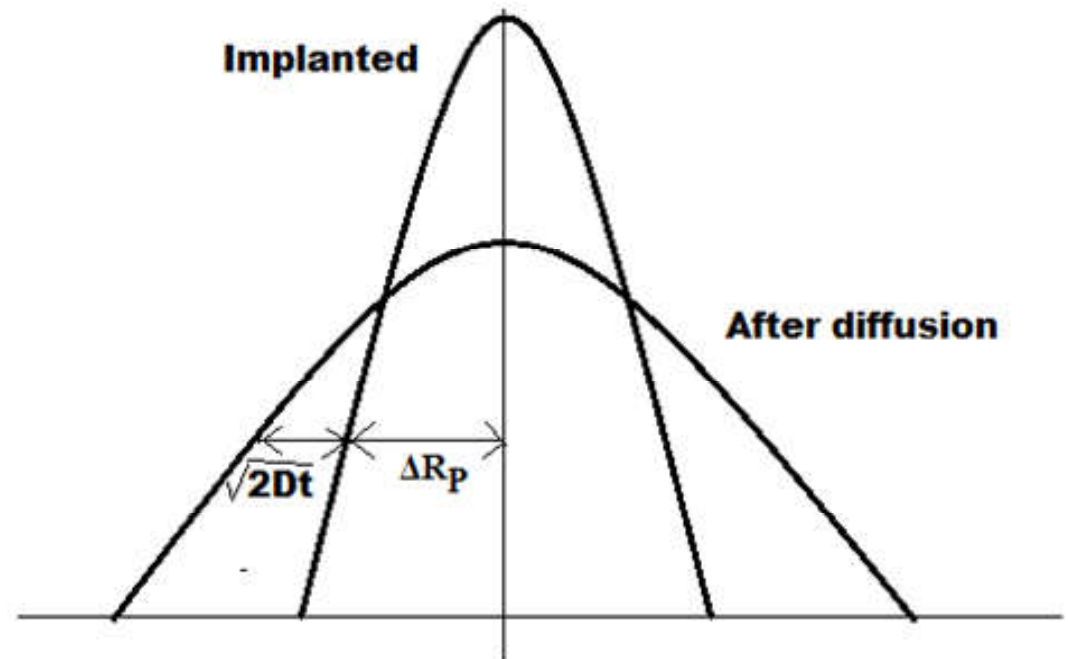


Figure 6.43 Evolution of Gaussian profile after annealing. The Gaussian preserves its shape as it diffuses in an infinite medium.

Effect of Annealing

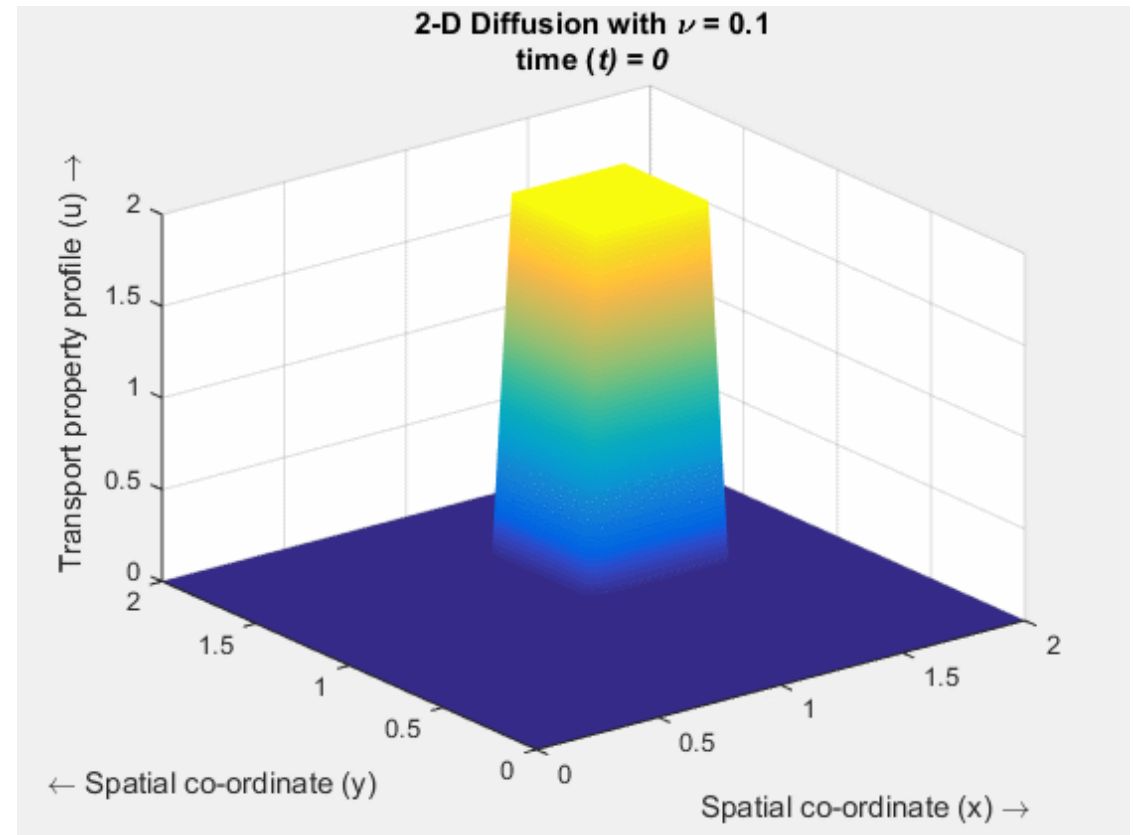
$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial x^2}$$

$$C(x, t = 0) = C_0(x)$$

$$C(x = +\infty, t > 0) = 0$$

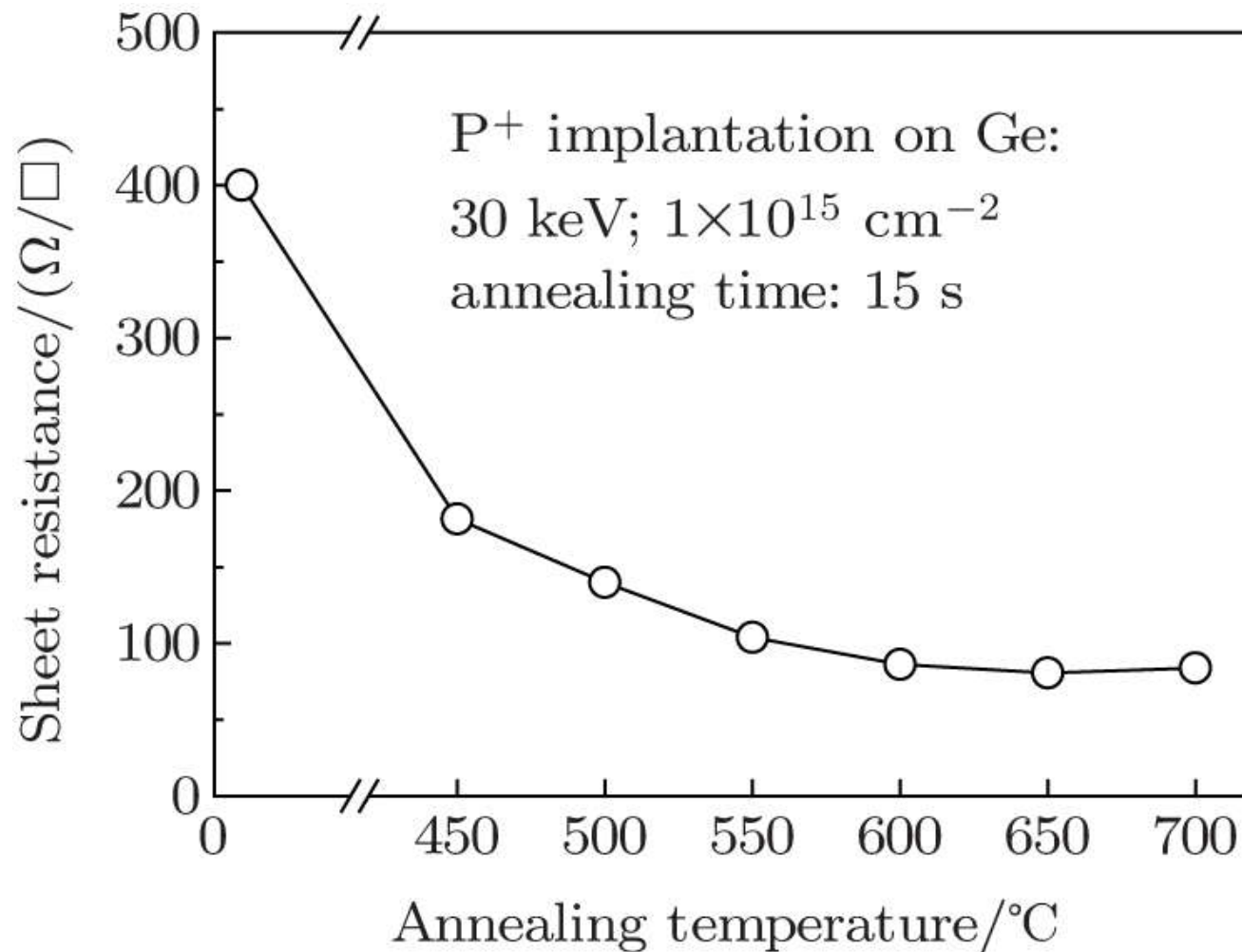


$$C(x, t) = \frac{Q}{\sqrt{2\pi(\Delta R_p^2 + 2Dt)}} \cdot \exp\left[-\frac{(x - R_p)^2}{2(\Delta R_p^2 + 2Dt)}\right]$$



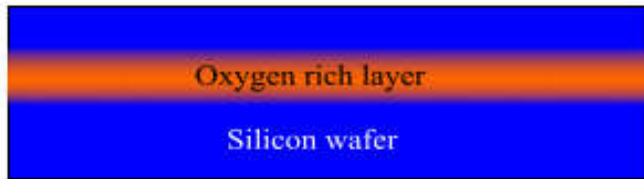
Effect of Annealing

'activate' dopants by annealing

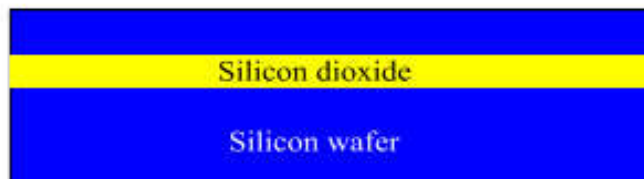
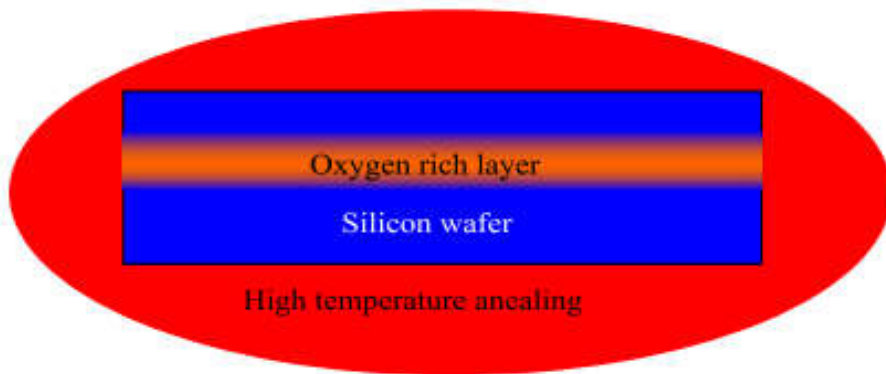


Make Silicon-on-Insulator (SOI)

↓ ↓ ↓ ↓ ↓ ↓ ↓ oxygen ion implant



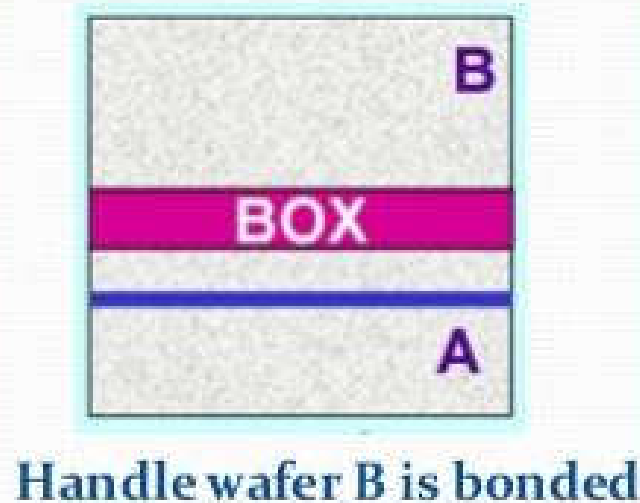
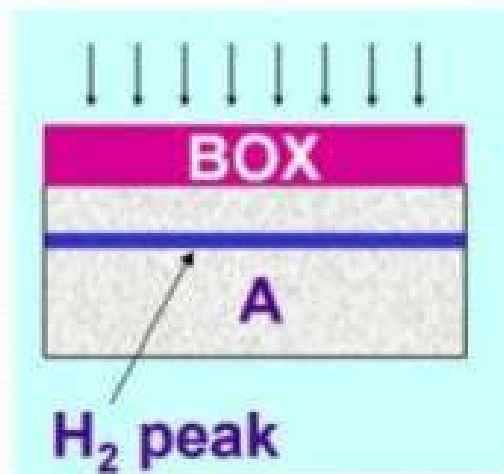
'SIMOX'
Separation by IMplanted OXYgen



Make Silicon-on-Insulator (SOI)

'Smart-Cut'

Hydrogen implantation
through thermal oxide
dose $\sim 1-5 \times 10^{16} \text{ cm}^{-2}$



At $\sim 400-600^\circ\text{C}$ wafer
A separates from B
at H_2 peak



After low temperature splitting, SOI wafer (B) is annealed $\sim 1100^\circ\text{C}$ to strengthen the bond, whereas wafer A is reused. SOI film thickness set by H_2 implant energy and BOX thickness

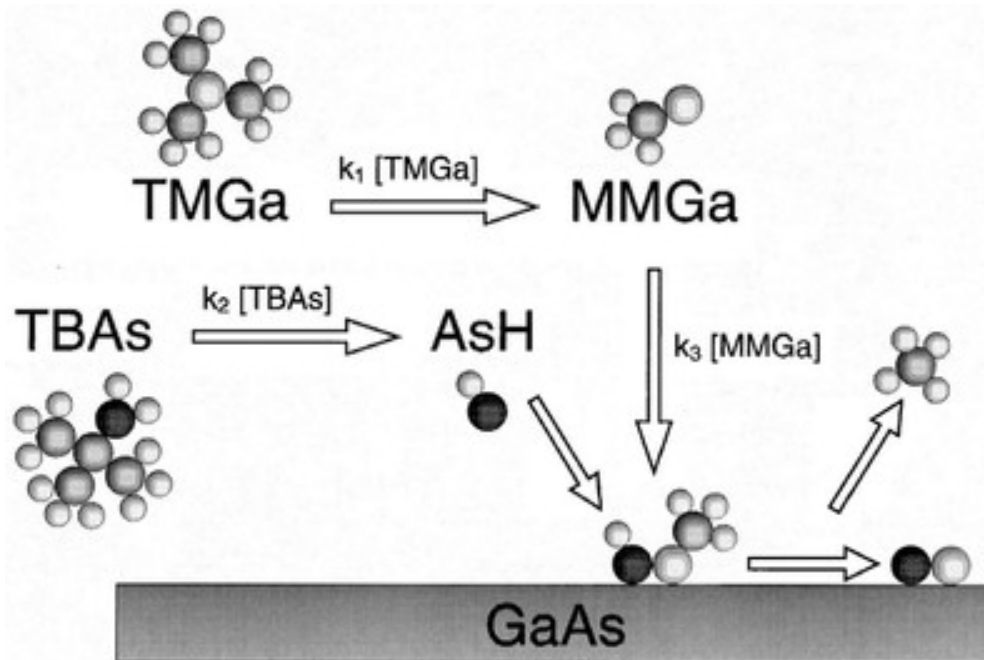
Doping Methods

- Thermal diffusion 热扩散
- Ion implantation 离子注入
- In situ growth 原位掺杂

Doping of Gallium Arsenide (GaAs)

■ GaAs growth

- MOCVD: $\text{Ga}(\text{CH}_3)_3 + \text{AsH}_3 \rightarrow \text{GaAs} + 3\text{CH}_4$
- add dopant gas: SiH_4 , Mg, Zn, ...
- vertical structures with high quality thin-films

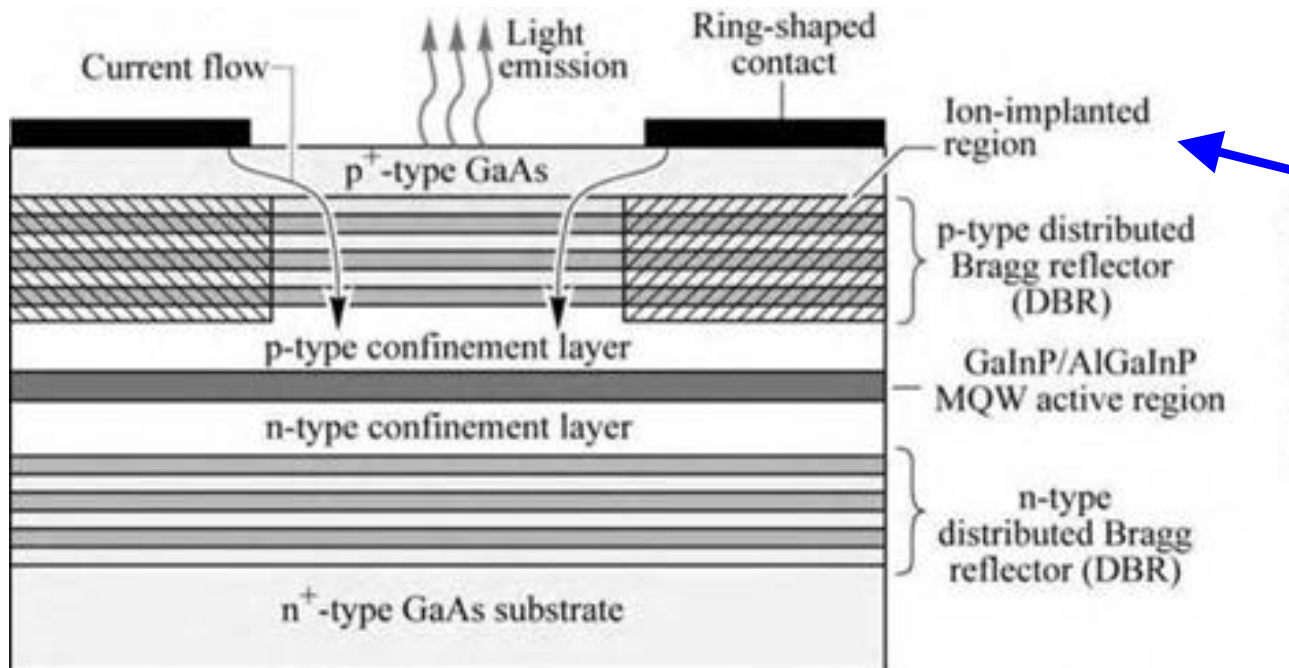
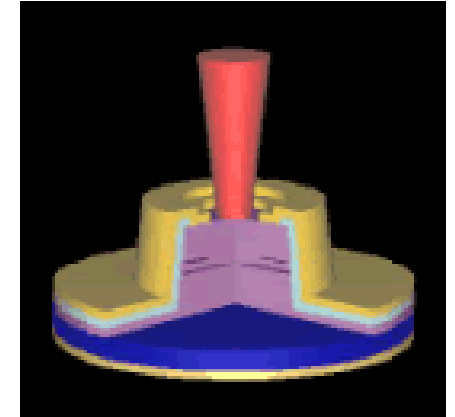


materials	thickness (nm)	doping (cm^{-3})	dopant
n+ GaAs contact	200	$6\text{e}18$	Si
n+ <u>InGaP</u> window	30	$2\text{e}18$	Si
n+ <u>GaAs</u> emitter	100	$2\text{e}18$	Si
p- <u>GaAs</u> base	2500	$1\text{e}17$	Zn
p+ $\text{Al}_{0.3}\text{Ga}_{0.7}\text{As}$ BSF	100	$5\text{e}18$	Mg
p+ <u>GaAs</u> substrate	-	$5\text{e}18$	Mg

Example: GaAs solar cell

GaAs VCSEL

- Vertical Cavity Surface Emitting Laser
 - growth with in situ doping
 - isolation by ion implantation

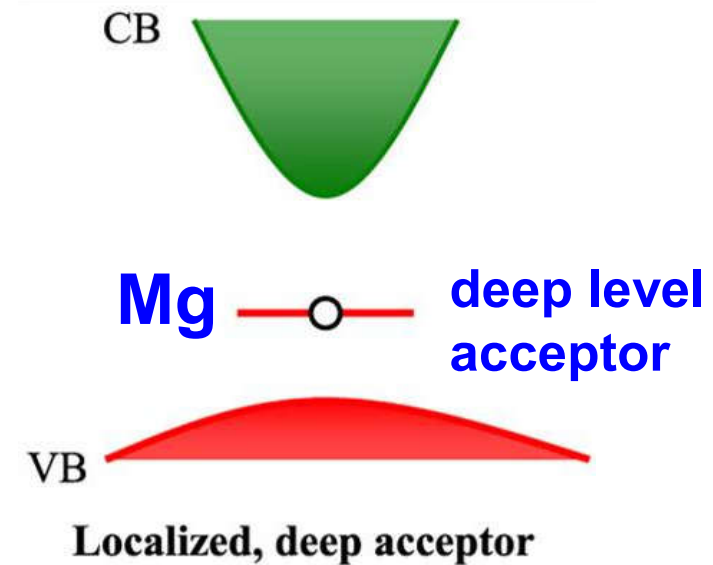


ion implanted (H⁺, O⁻, ...) region for isolation

highly damaged and resistive region

Doping of Gallium Nitride (GaN)

- n-GaN is easy
 - use Si to replace Ga
- p-GaN is very difficult
 - use Mg to replace Ga, but ...

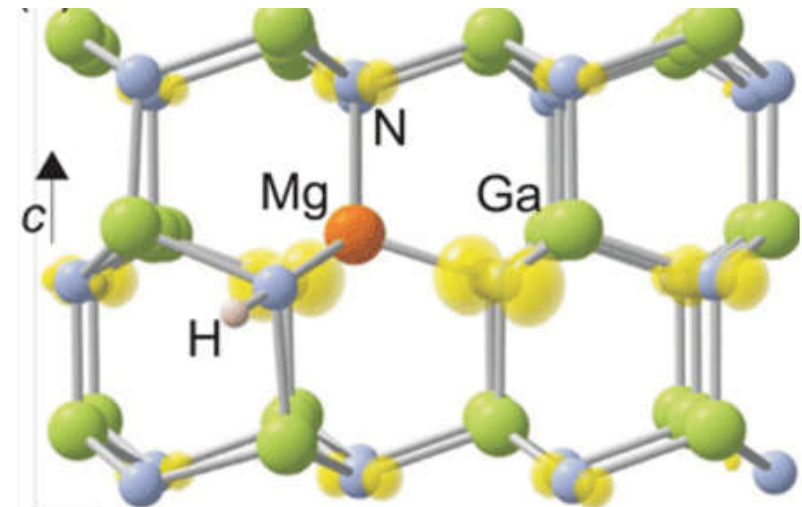


H. Amano, *et al.*, *Jpn. J. Appl. Phys.* **28**, L2112 (1989)
 S. Nakamura, *et al.*, *Appl. Phys. Lett.* **64**, 1687 (1994)



I. Akasaki H. Amano S. Nakamura

2014 Nobel Prize in Physics



hydrogen reduces distortion

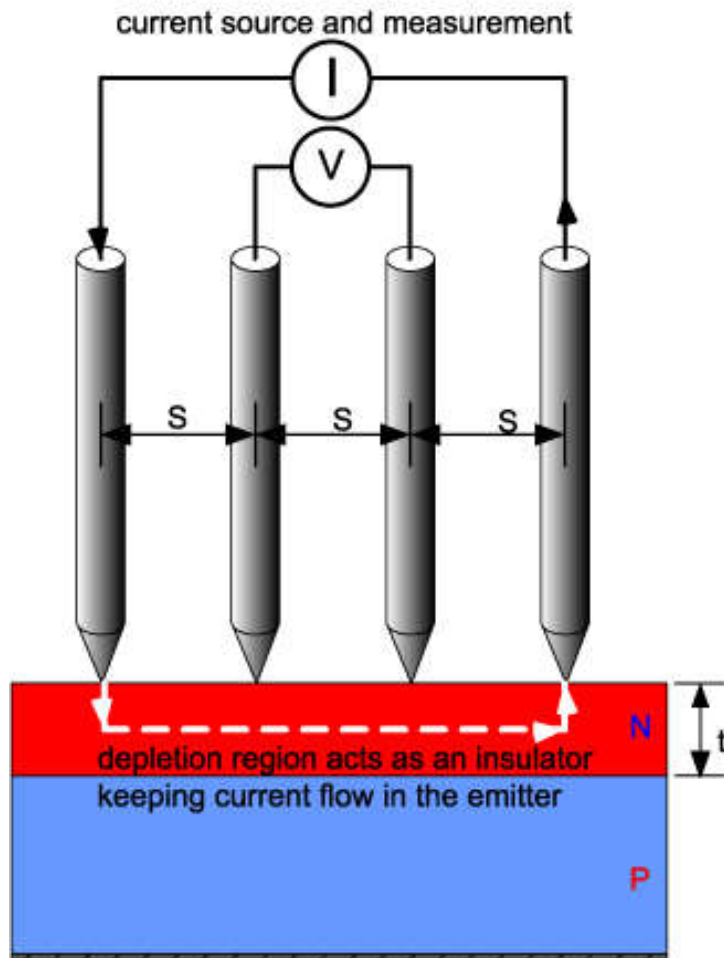
Doping Measurement

Commonly used diffusion profile measurement techniques

Profile techniques	Characteristics
Capacitance-Voltage	Carrier concentration at the edge of the depletion layer of a pn junction. Maximum total dopants 2×10^{12} atoms/cm ² .
Differential conductance	Resistivity and Hall effect mobility of net electrically active species. Requires thin-layer removal, concentration range from 10^{20} to 10^{18} atoms/cm ³ .
Spreading resistance	Resistance on angle-beveled sample. Good for comparison with known profiles and quick semi quantitative evaluation. $x_j \geq 1\mu\text{m}$.
SIMS	High sensitivity on many elements; for B and As detection limit is $5 \times 10^{15}\text{cm}^{-3}$. Capable of measuring total dopant profiles in 1000Å range. Needs standards.
Radioactive tracer analysis	Total concentration. Lower limit is 10^{15}cm^{-3} . Limited to radioactive elements with suitable half-life times: P, As, Sb, Na Cu, Au, etc.
Rutherford backscattering	Applicable only for elements heavier than Si.
Nuclear reaction	Measures total boron through $^{10}\text{B}(n, ^4\text{He})^7\text{Li}$, or $^{11}\text{B}(p, \alpha)$. Needs Van de Graaff generator.

Resistivity

Four Point Probe Measurement



conductivity

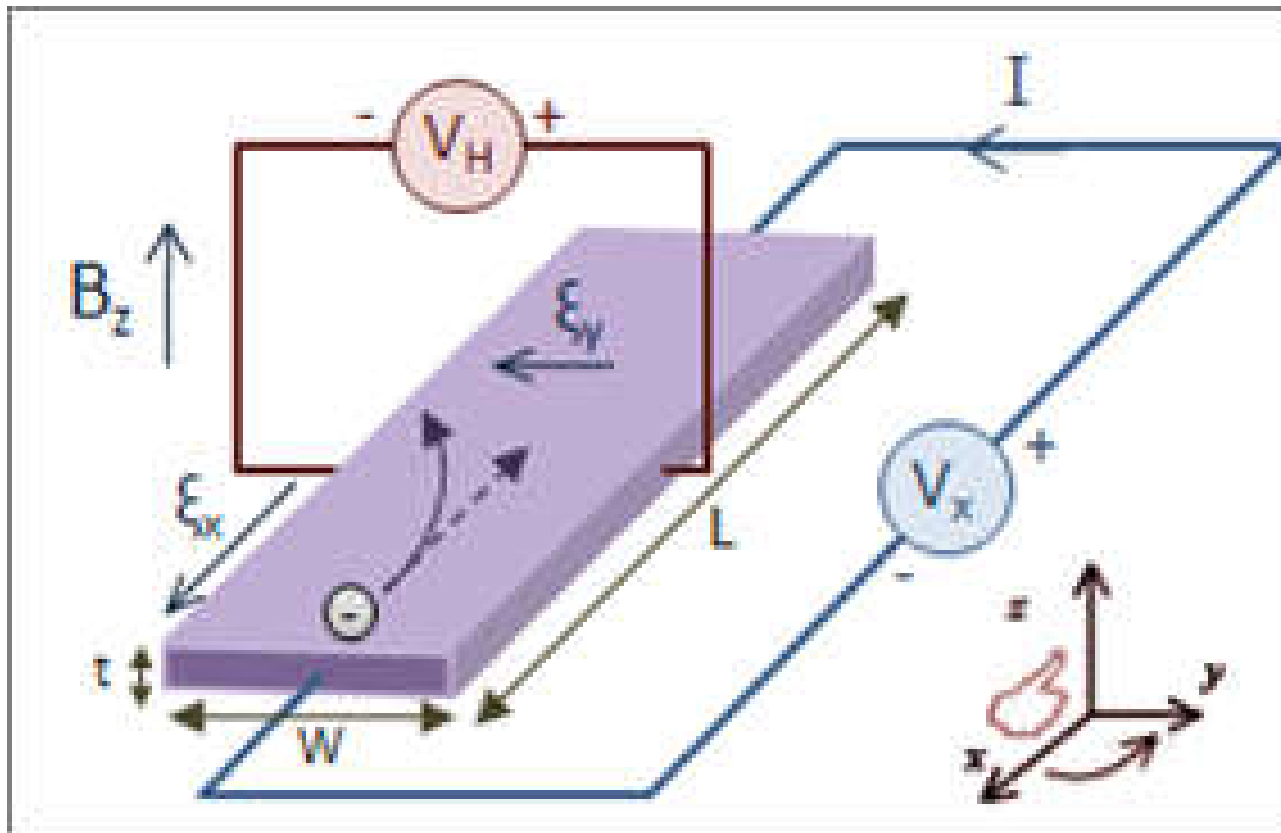
$$\sigma(x) = e \cdot \mu \cdot C(x) = \frac{1}{\rho(x)}$$

sheet resistance

$$R_s = \frac{\rho}{x} = \frac{1}{\int_0^t \sigma(x) dx}$$

Hall Effect

- Measure doping type and concentration



$$V_H = \frac{I_x \cdot B_z}{C \cdot t \cdot e}$$

n-type: $V_H > 0$

p-type: $V_H < 0$

SIMS

- **SIMS: Secondary Ion Mass Spectroscopy**
 - equipment similar with ion implantation

